

Distributed Algorithms 2020

2

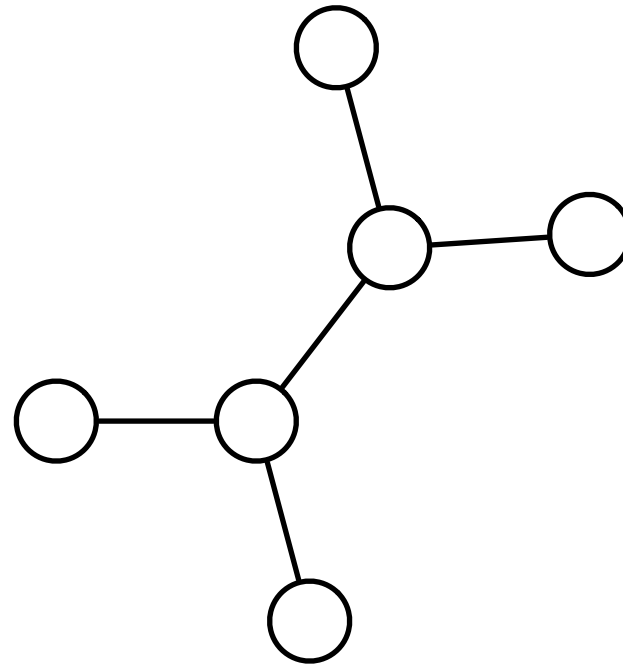
Graph-theoretic foundations

Graphs in this course

- Defining:
 - models of distributed computing
 - what we want to solve
 - what are the assumptions
- Designing & analyzing algorithms
- Proving impossibility results
- Often: *graph* \approx *network*, *node* \approx *computer*

Quiz

- Graph where maximal independent sets are never minimum dominating sets?



Please do not confuse

- **Maximal**

- not a subset of another solution
- very easy to find: add greedily

- **Maximum**

- largest possible solution
- often hard to find

Please do not confuse

- **Minimal**

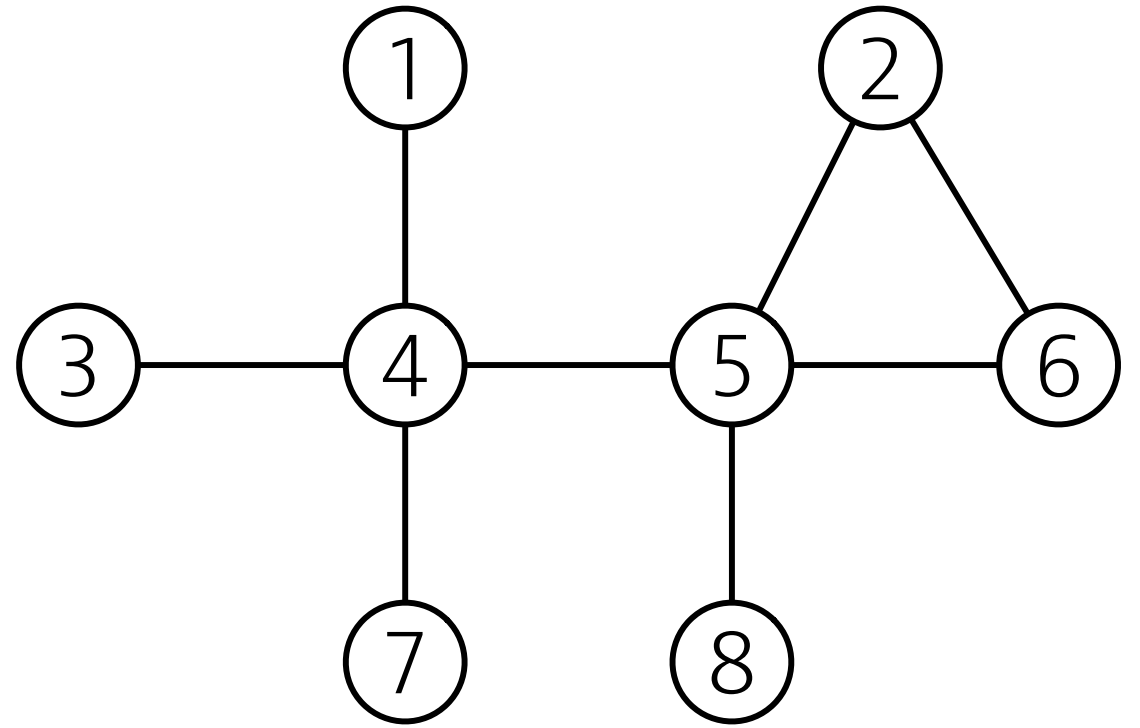
- not a superset of another solution
- very easy to find: remove greedily

- **Minimum**

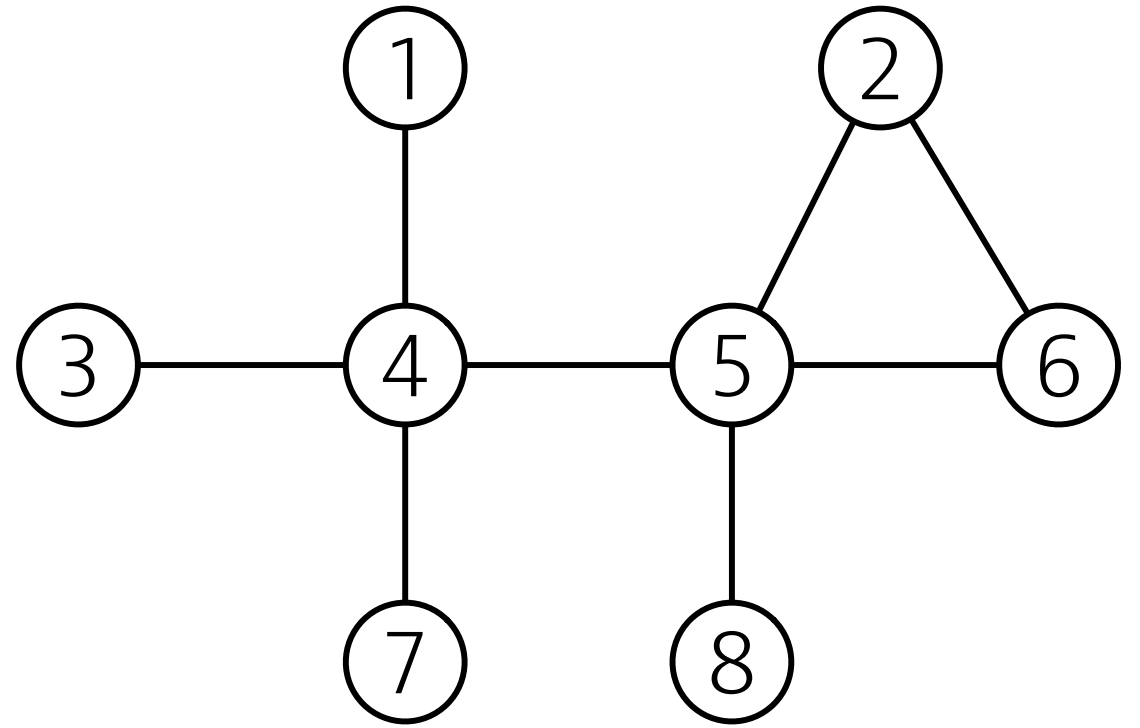
- smallest possible solution
- often hard to find

Q & A

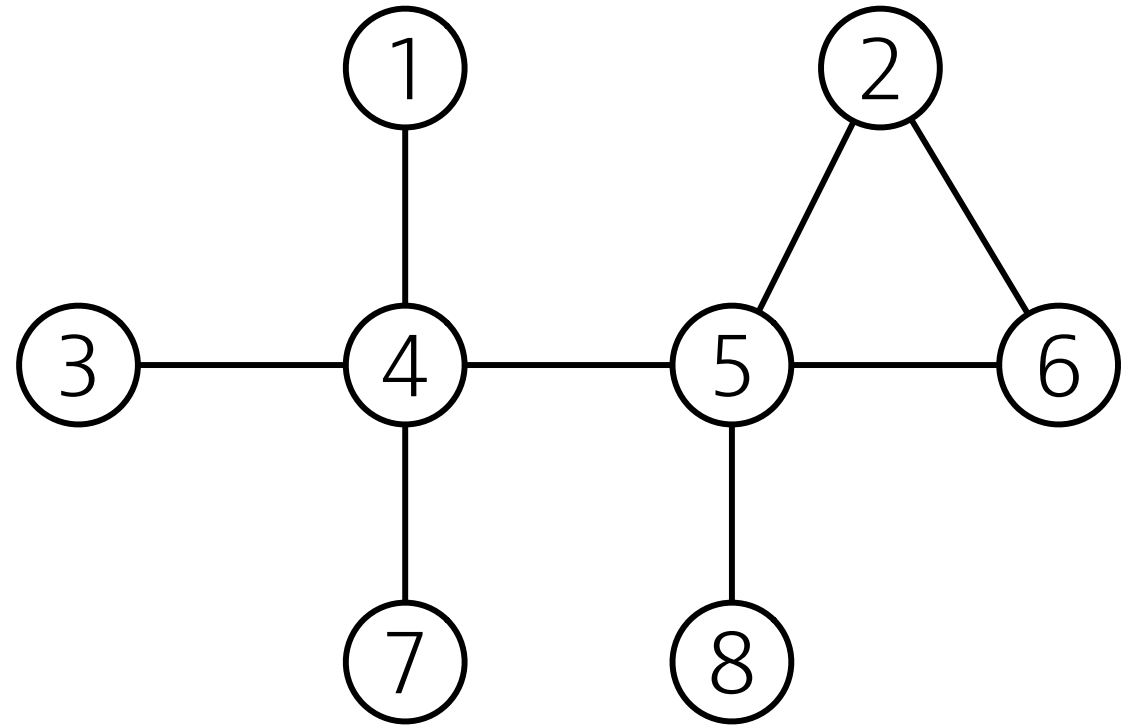
**Please answer
on Slack...**



Minimum
vertex cover

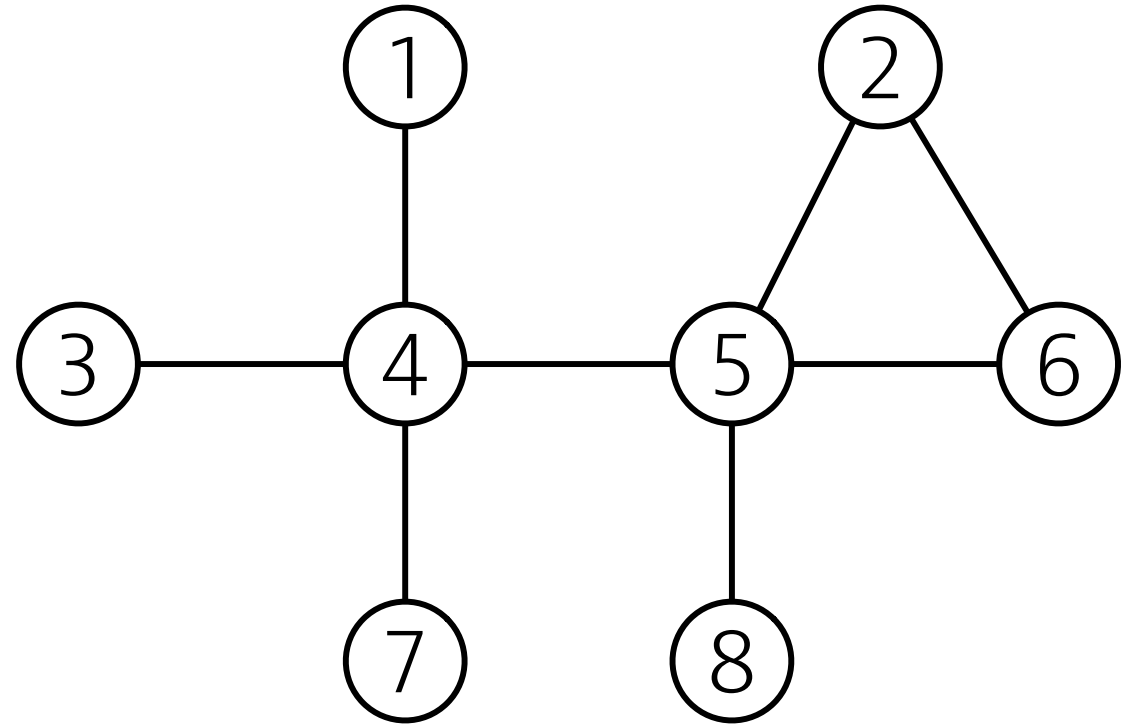


Minimum
dominating set

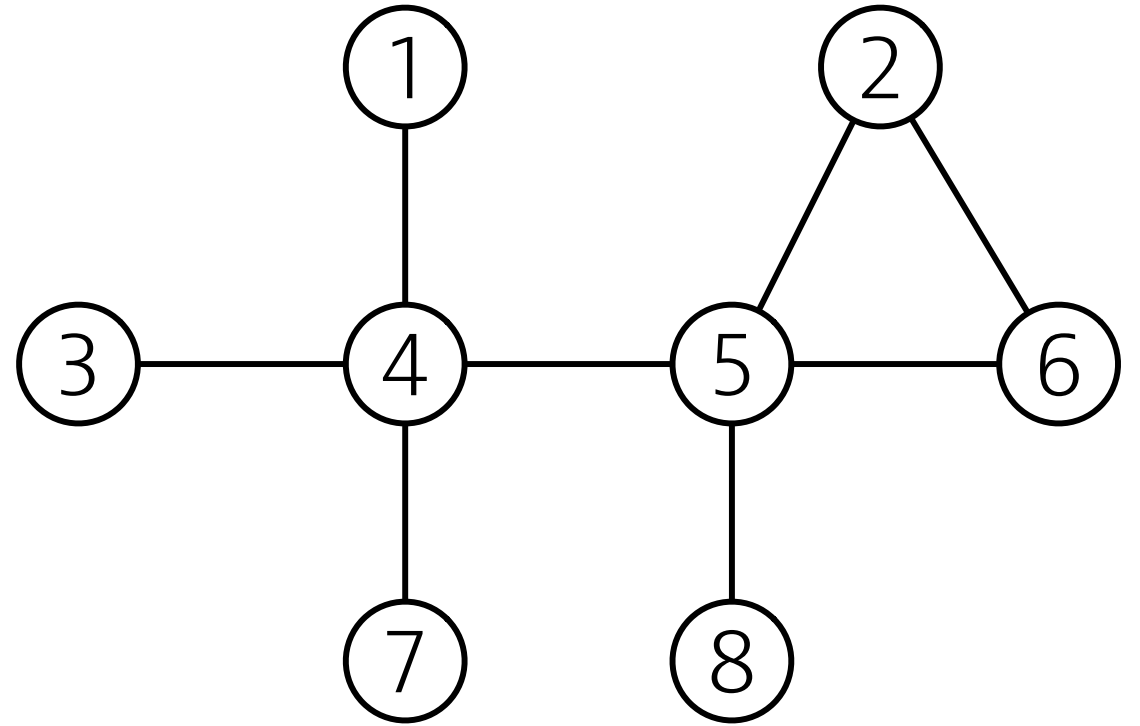


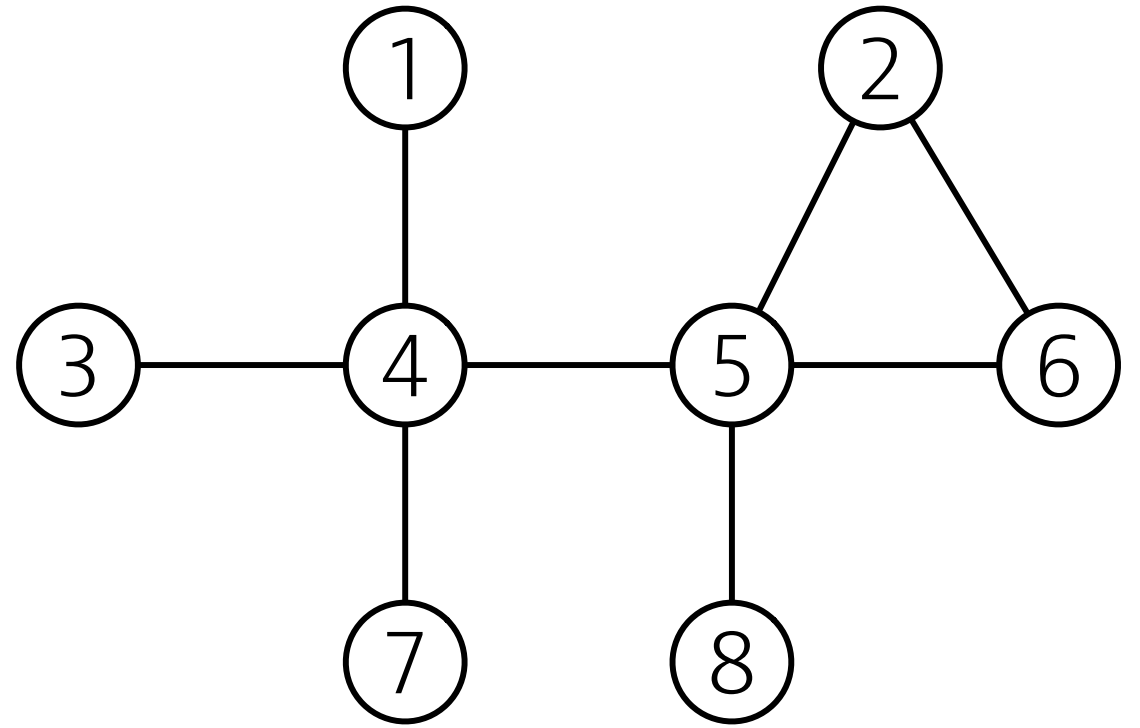
Maximum
independent set

Smallest
set of nodes
that is both
an independent set
and a dominating set

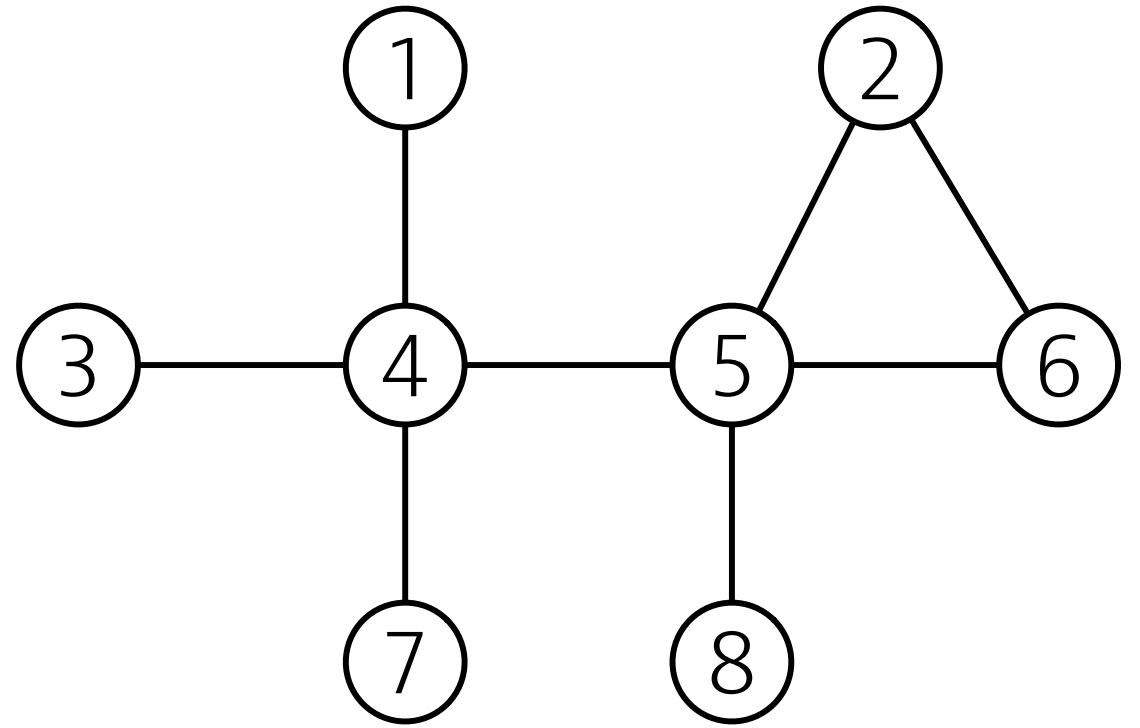


Largest
set of nodes
that is both
an independent set
and a dominating set

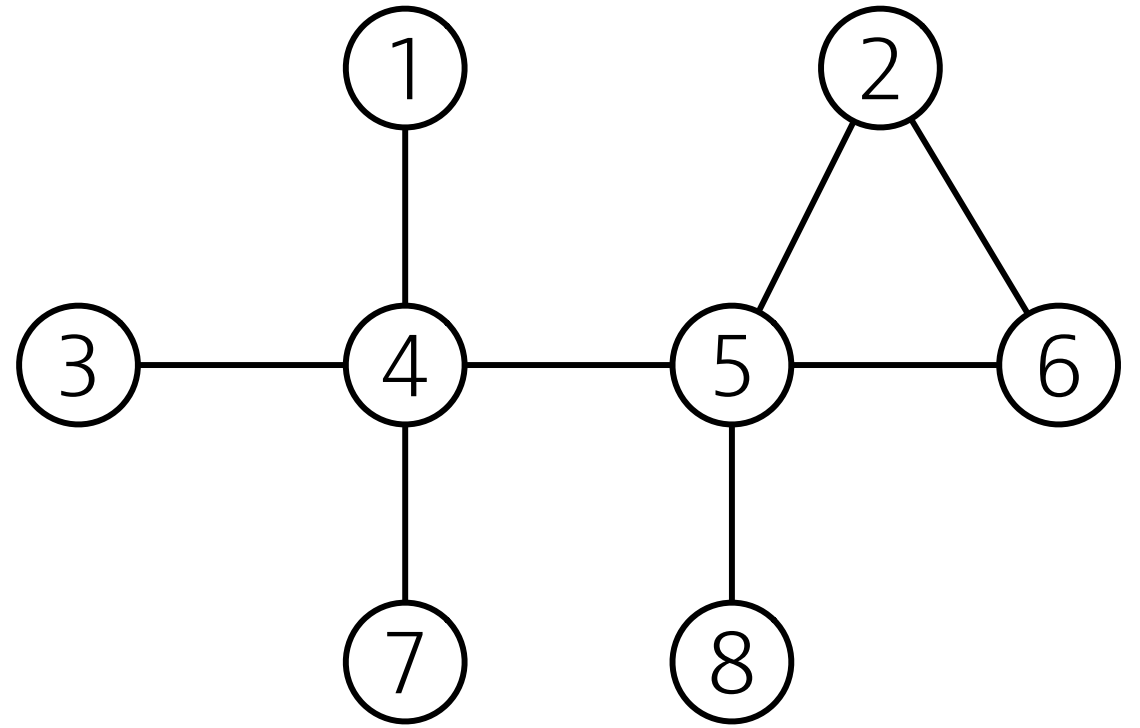




Maximum
matching

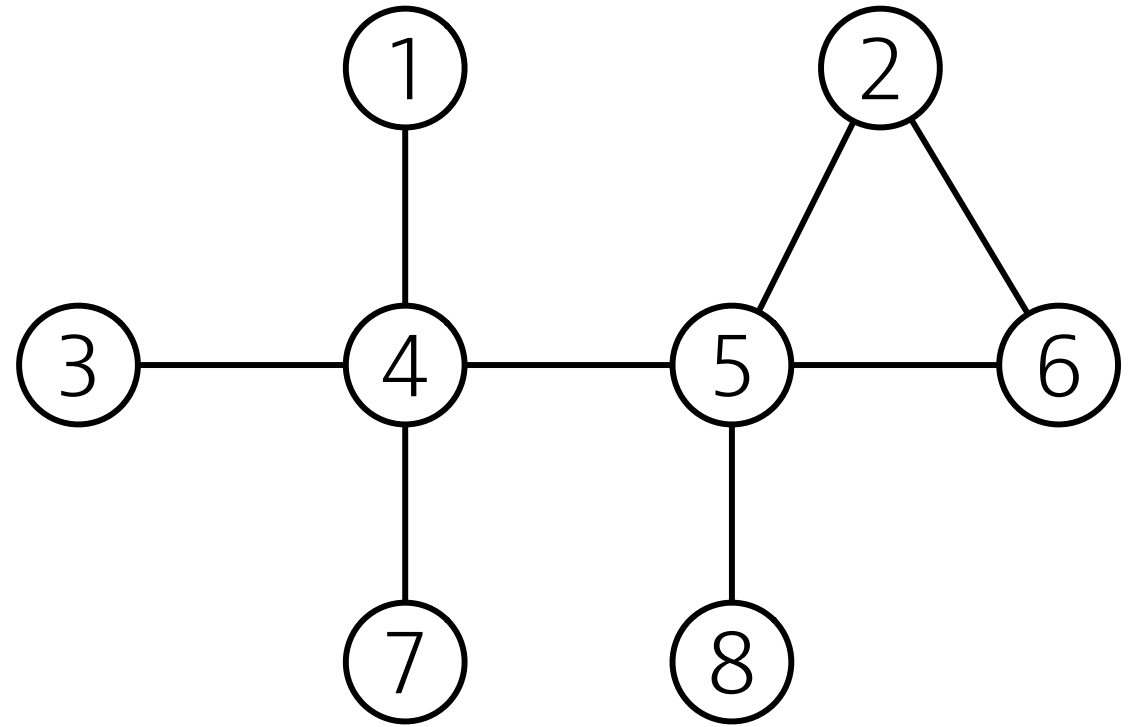


Minimum
edge cover

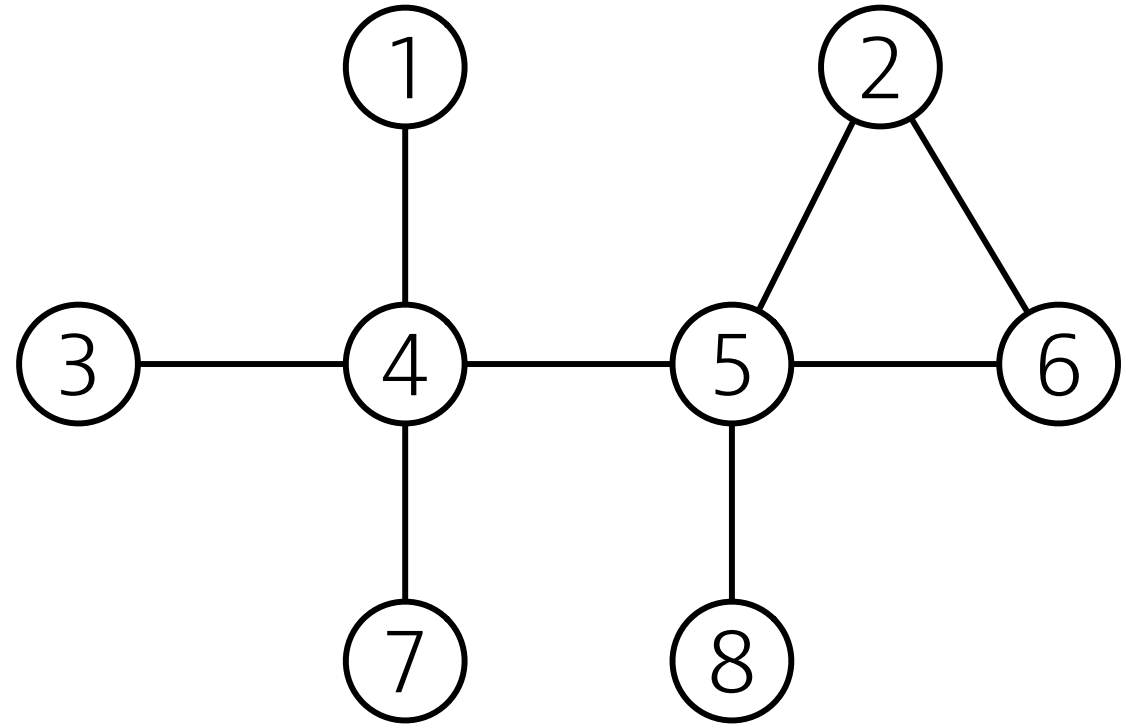


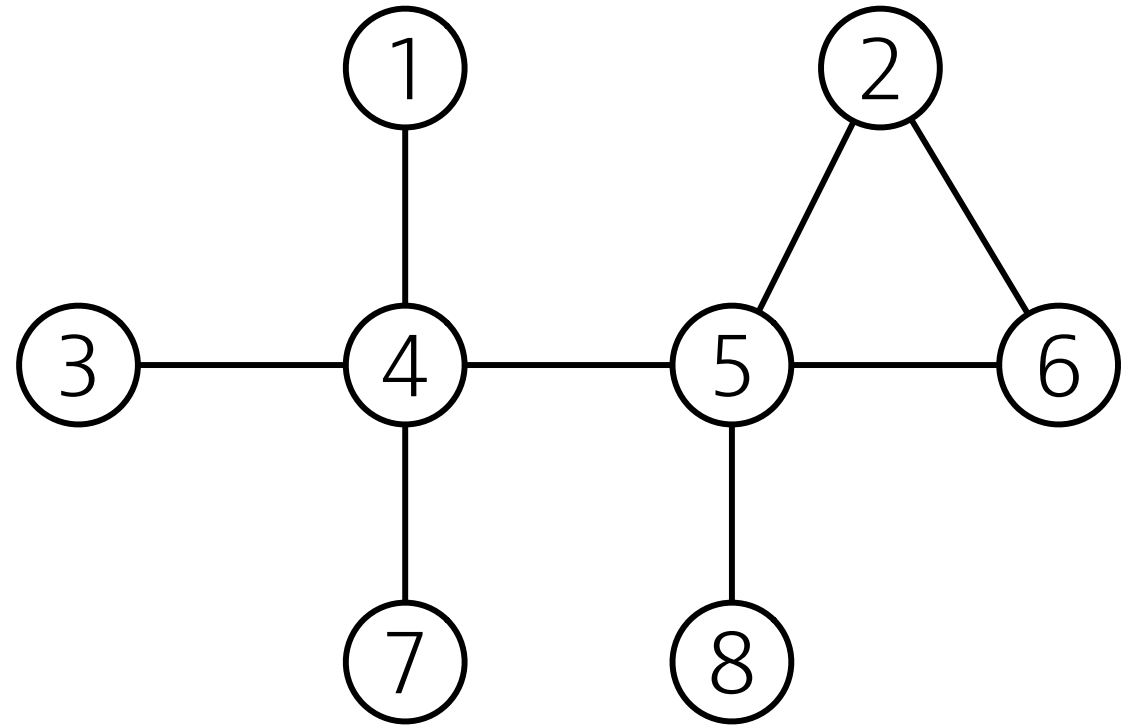
Minimum
edge dominating set

Smallest
set of edges
that is both
a matching and
an edge dominating set

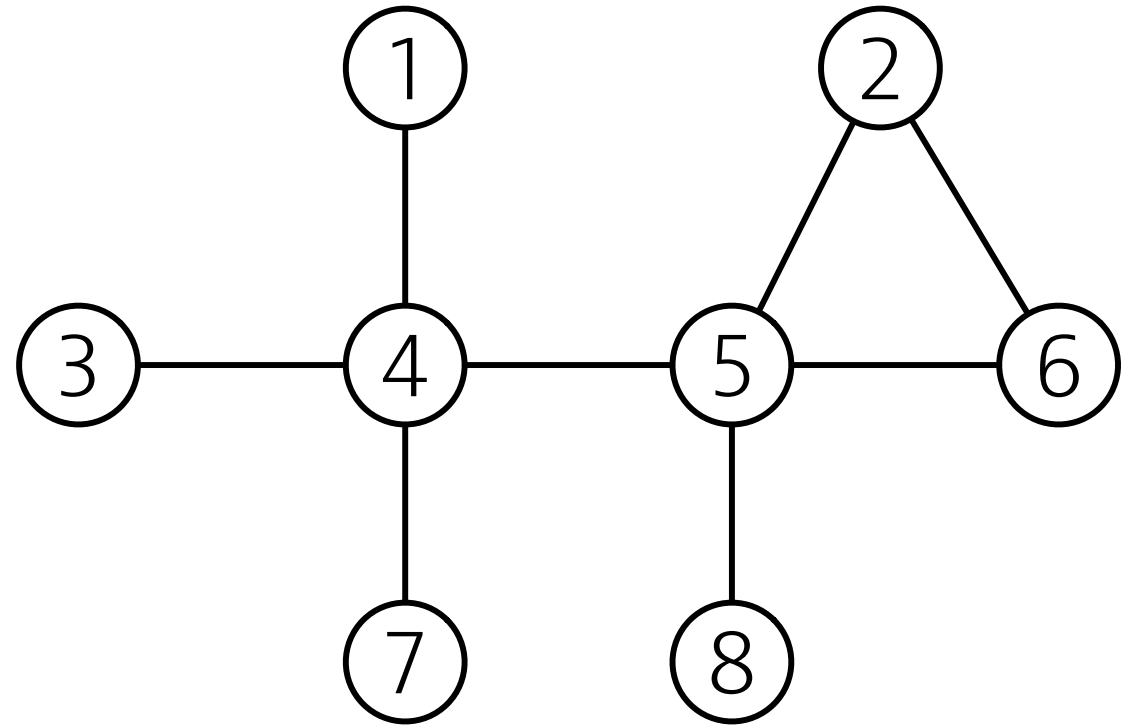


Largest
set of edges
that is both
a matching and
an edge dominating set



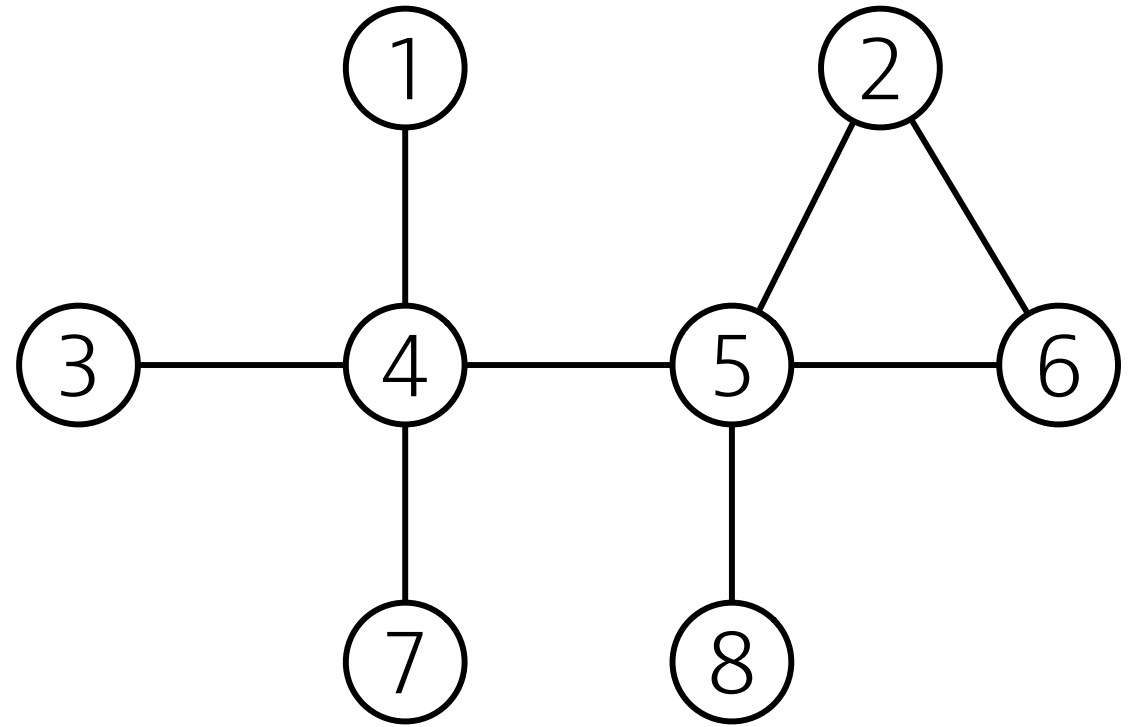


Minimum
edge dominating set
that is not a matching

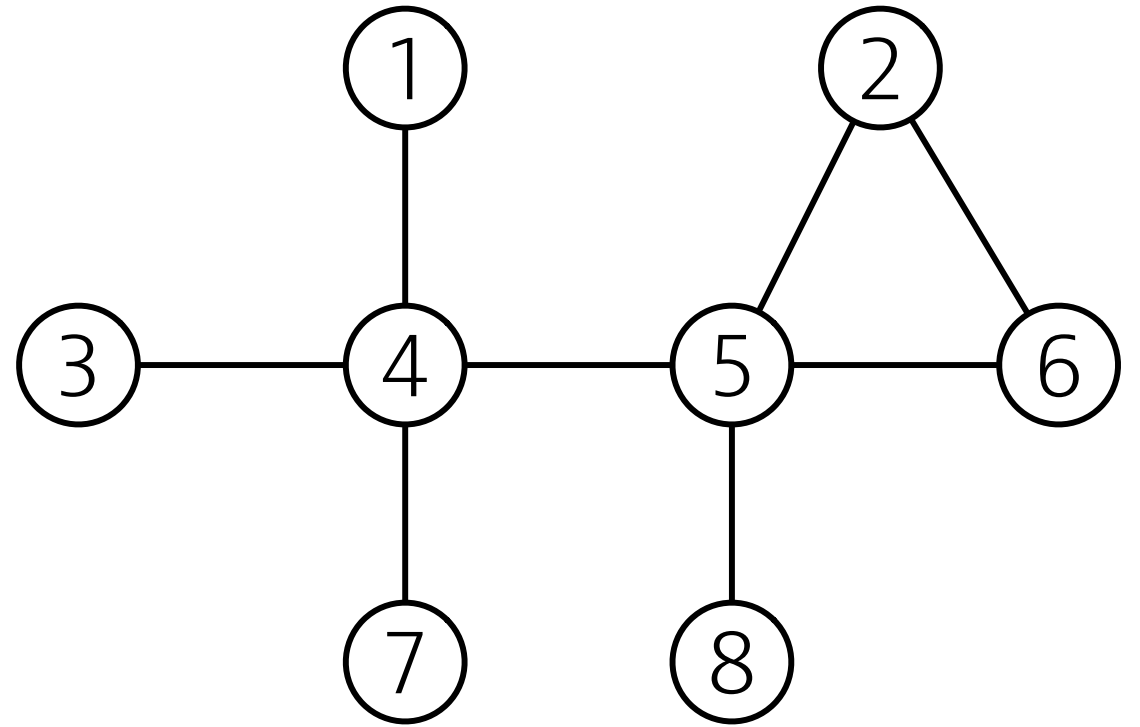


Largest set of nodes that induces a bipartite subgraph

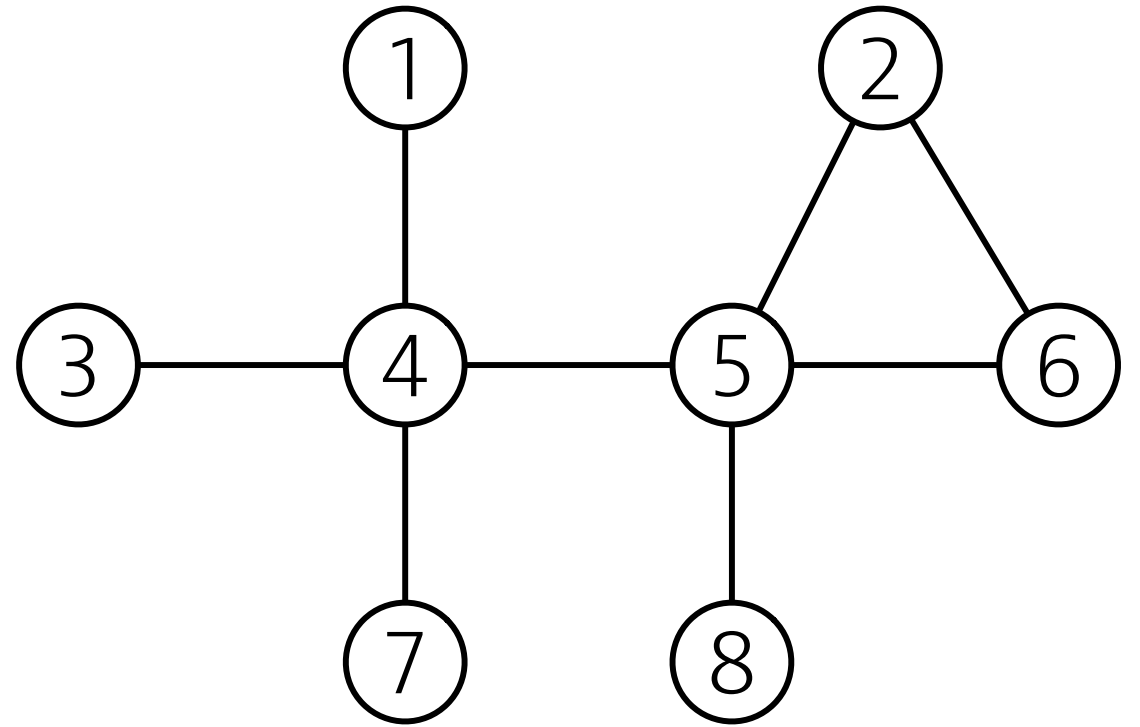
Largest
set of edges
that induces
a subgraph with
2 connected components

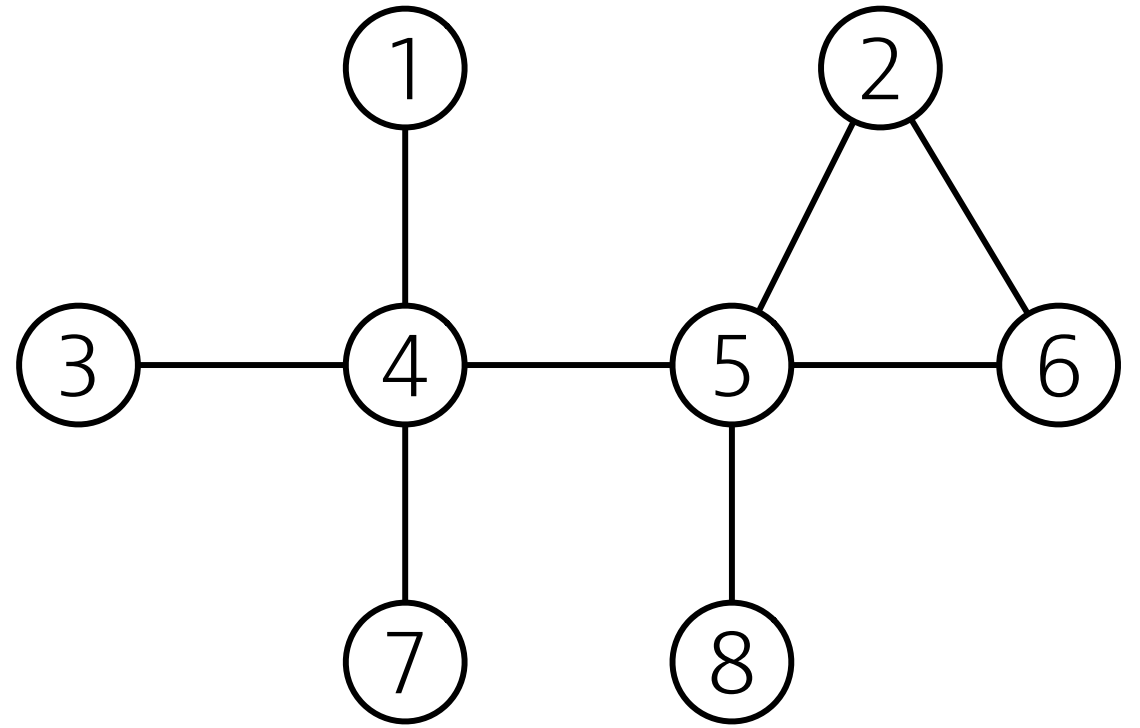


Largest
set of nodes
that induces
a subgraph of
maximum degree 2



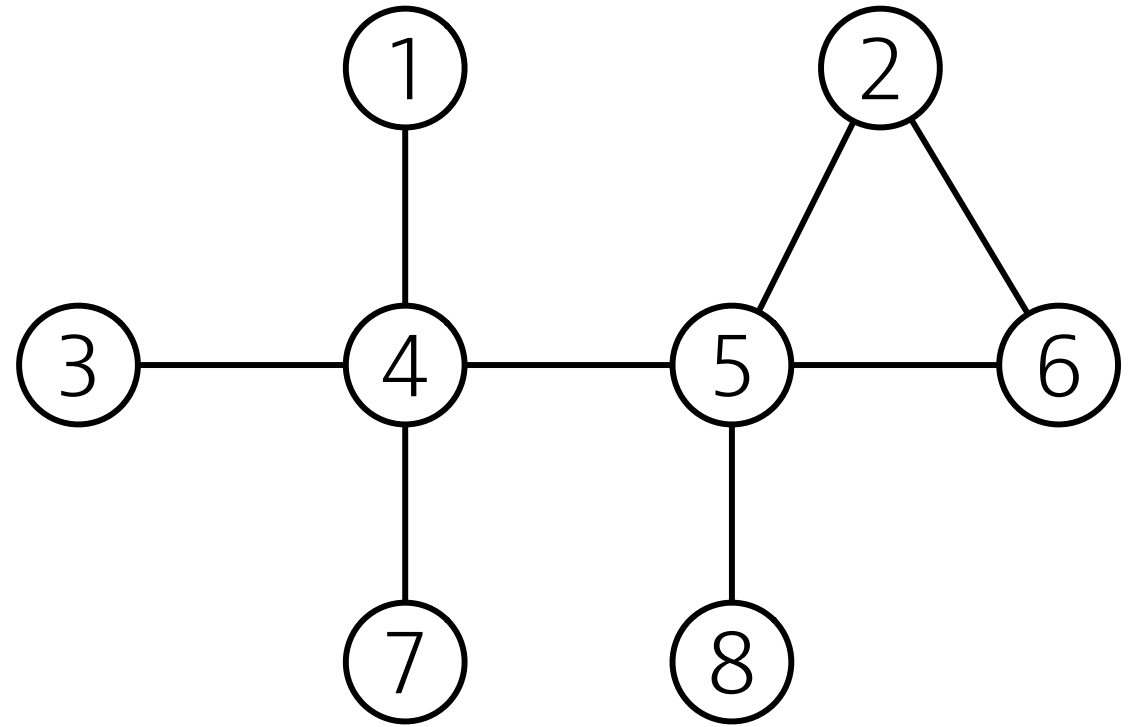
Largest
set of edges
that induces
a subgraph of
maximum degree 2





Set of nodes
that induces
a 2-regular subgraph

Nodes u
and v such
that the distance
from u to v equals
the diameter of the graph



Group work