

# Distributed Algorithms 2020

8 Local neighborhoods

# High-level plan

Algorithm  $A$  runs in  **$T$  rounds** and solves problem  $X$

→  $A$  is a **mapping from radius- $T$  neighborhoods** to local outputs

Such a mapping cannot solve  $X$  correctly

→ Problem  $X$  is not solvable in  $T$  rounds

# Example: coloring

- **Problem:** find a vertex coloring with the smallest possible number of colors
- **Proof:** *three different approaches!*

# Example: coloring

- **Idea 1:** consider a path, *fix solutions in two neighborhoods*, construct another path

# Example: coloring

- **Idea 2:** consider an odd cycle, *look at a node that outputs "3"*, construct a path

# Example: coloring

- **Idea 3:** if we can 2-color paths locally, *then we can also 2-color odd cycles*

# What about...

- PN model?
- CONGEST model?
- Randomized algorithms?

# Example: leaf distance

- **Graph family:** trees
- **Model:** LOCAL
- **Input:** unique IDs and value of  $n$
- **Output:** distance to the nearest leaf node



# Example: leaf distance

# Example: is it a forest?

- **Input is a forest:** *all* nodes output "yes",  
**otherwise:** *at least one* node outputs "no"
- **Questions:**
  - is this solvable in PN, and how fast?
  - is this solvable in LOCAL, and how fast?
  - does it help if we know  $n$ ?

# Example: is it a forest?

- PN,  $n$  is not known?

# Example: is it a forest?

- PN,  $n$  is known?

# Example: is it a forest?

- LOCAL,  $n$  is not known?

# Example: is it a forest?

- LOCAL,  $n$  is known?