

Distributed Algorithms 2021



High-level plan

Algorithm A runs in **T rounds** and solves problem X

→ A is a mapping from radius-T neighborhoods to local outputs

Such a mapping cannot solve X correctly

 \rightarrow Problem X is not solvable in T rounds

- **Problem:** find a vertex coloring with the smallest possible number of colors
- Proof: three different approaches!

• Idea 1: consider a path, fix solutions in two neighborhoods, construct another path

• Idea 2: consider an odd cycle, look at a node that outputs "3", construct a path

Idea 3: if we can 2-color paths locally,
 then we can also 2-color odd cycles

What about...

- PN model?
- CONGEST model?
- Randomized algorithms?

Example: leaf distance

- Graph family: trees
- Model: LOCAL
- Input: unique IDs and value of n
- Output: distance to the nearest leaf node

Example: leaf distance

- Input is a forest: all nodes output "yes",
 otherwise: at least one node outputs "no"
- Questions:
 - is this solvable in PN, and how fast?
 - is this solvable in LOCAL, and how fast?
 - does it help if we know *n*?

• PN, *n* is not known?

• PN, *n* is known?

• LOCAL, *n* is not known?

• LOCAL, *n* is known?