

# Distributed Algorithms 2022

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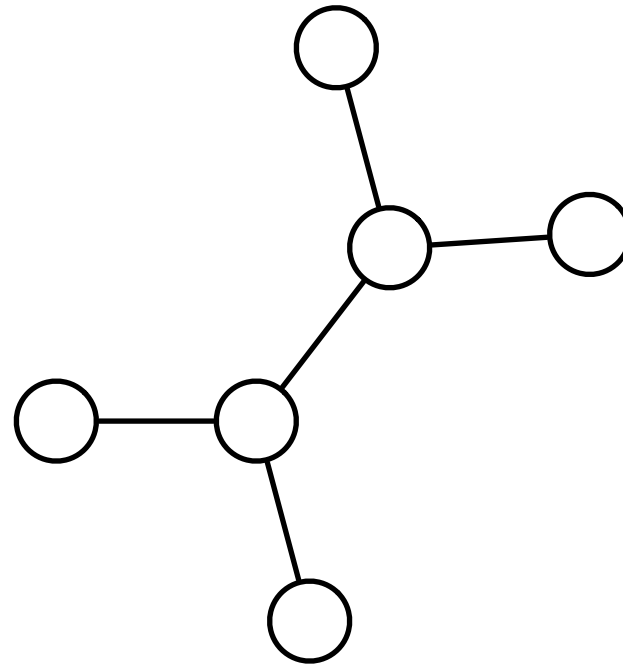
Graph-theoretic foundations

# Graphs in this course

- Defining:
  - models of distributed computing
  - what we want to solve
  - what are the assumptions
- Designing & analyzing algorithms
- Proving impossibility results
- Often: *graph*  $\approx$  *network*, *node*  $\approx$  *computer*

# Quiz

- Graph where maximal independent sets are never minimum dominating sets?



# Please do not confuse

- **Maximal**

- not a subset of another solution
- very easy to find: add greedily

- **Maximum**

- largest possible solution
- often hard to find

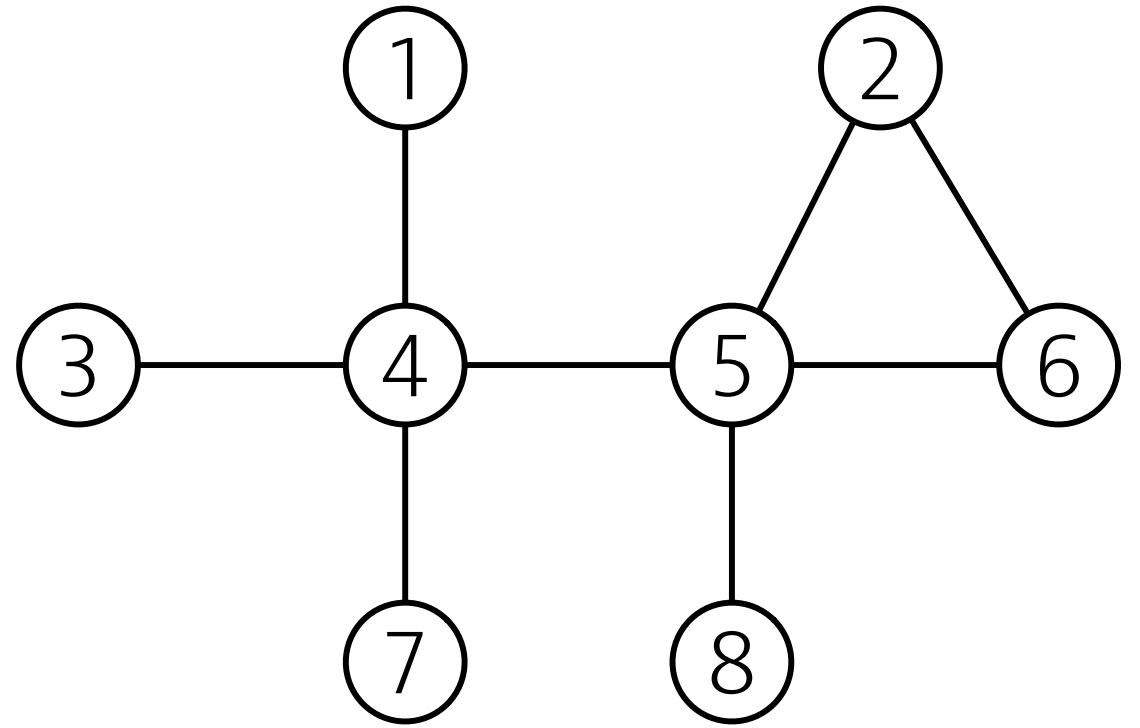
# Please do not confuse

- **Minimal**

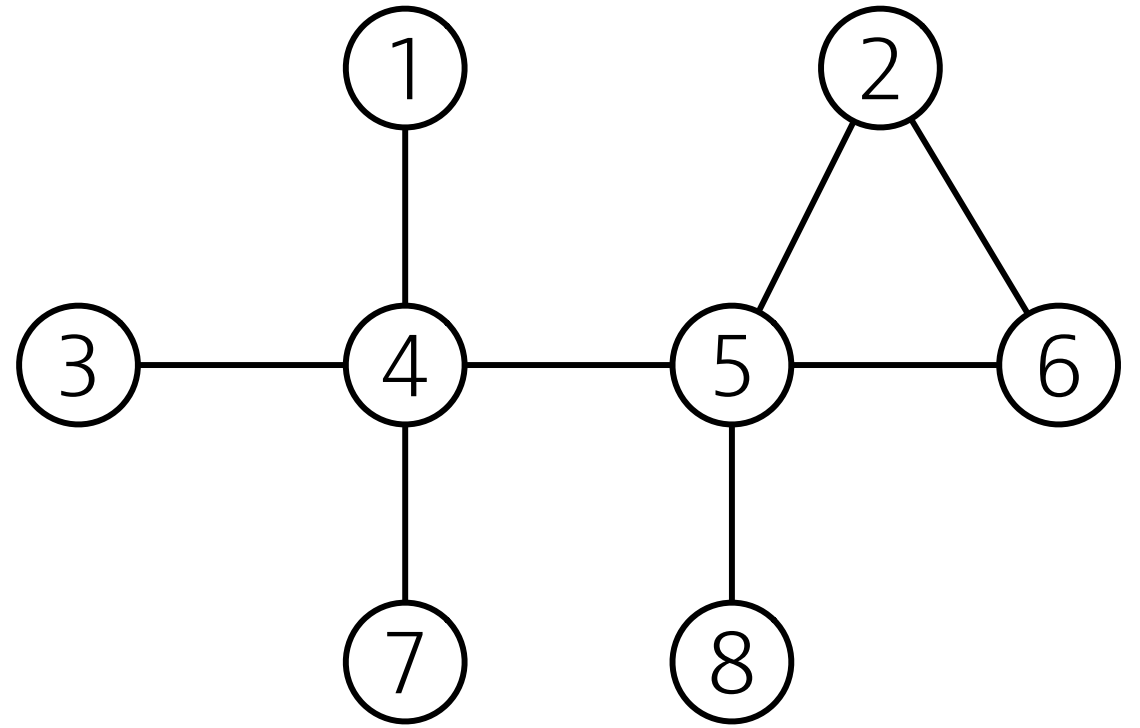
- not a superset of another solution
- very easy to find: remove greedily

- **Minimum**

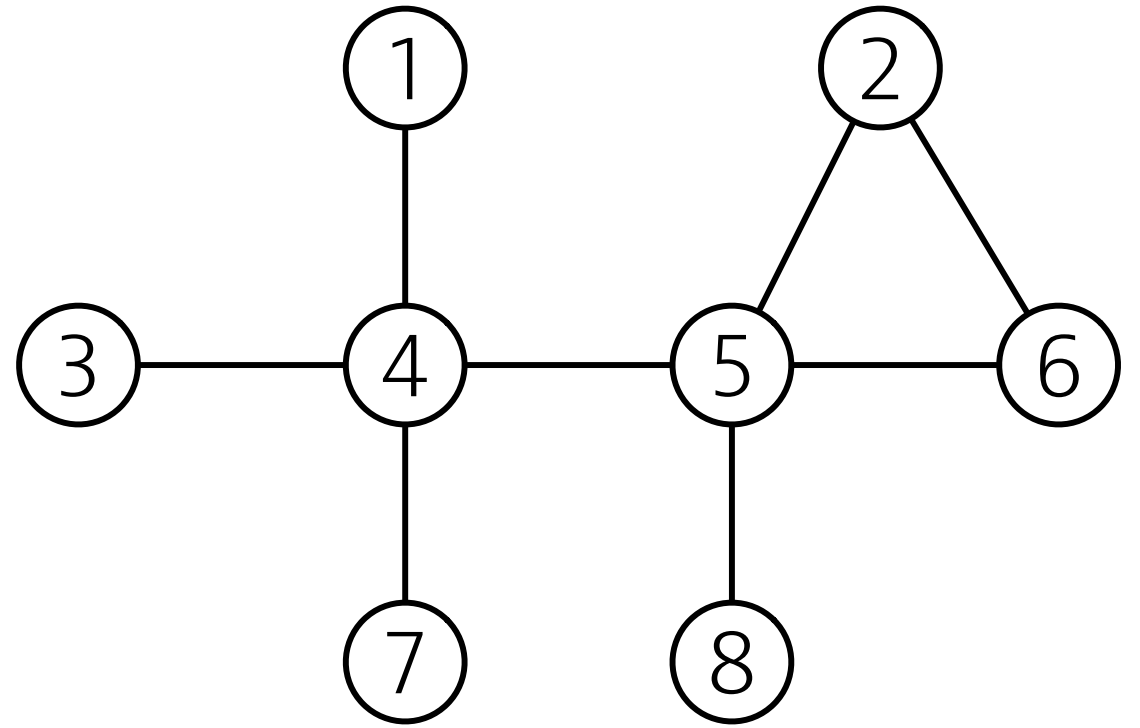
- smallest possible solution
- often hard to find



Minimum  
vertex cover



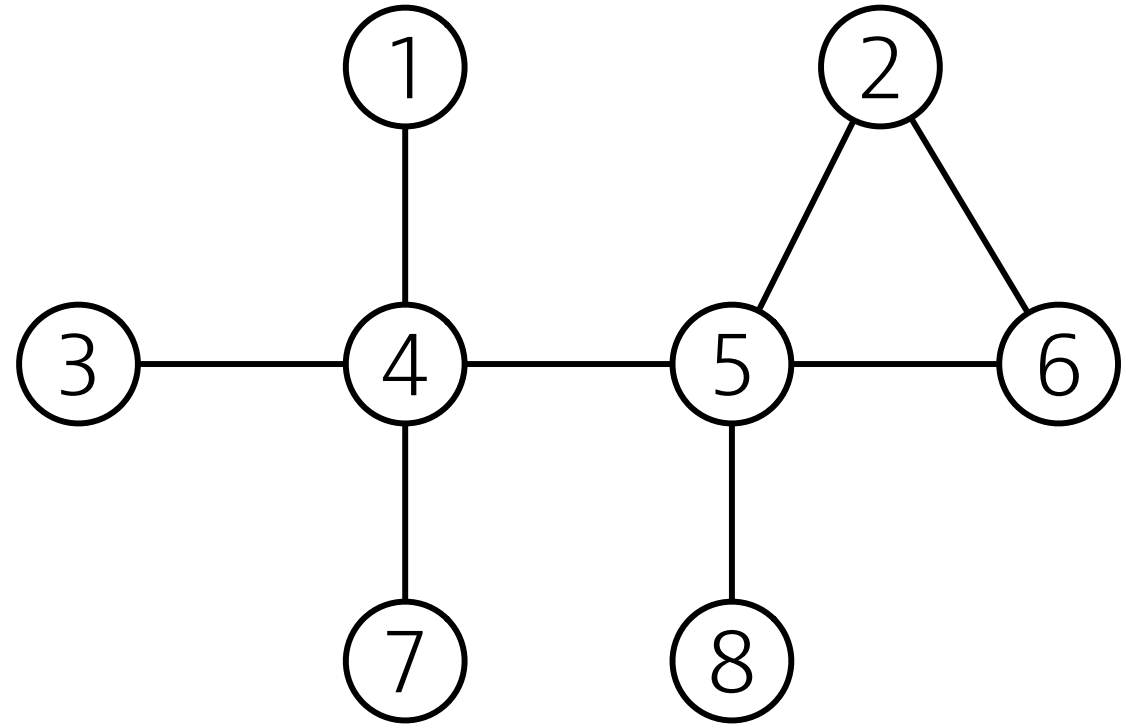
Minimum  
dominating set



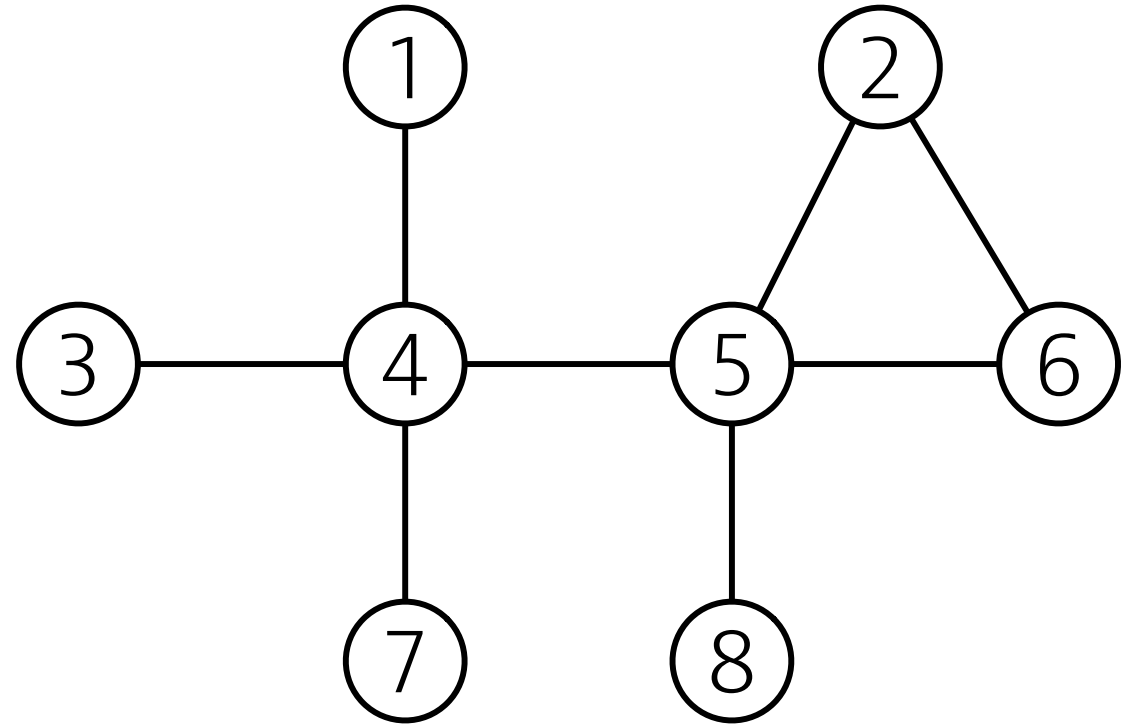
Maximum  
independent set

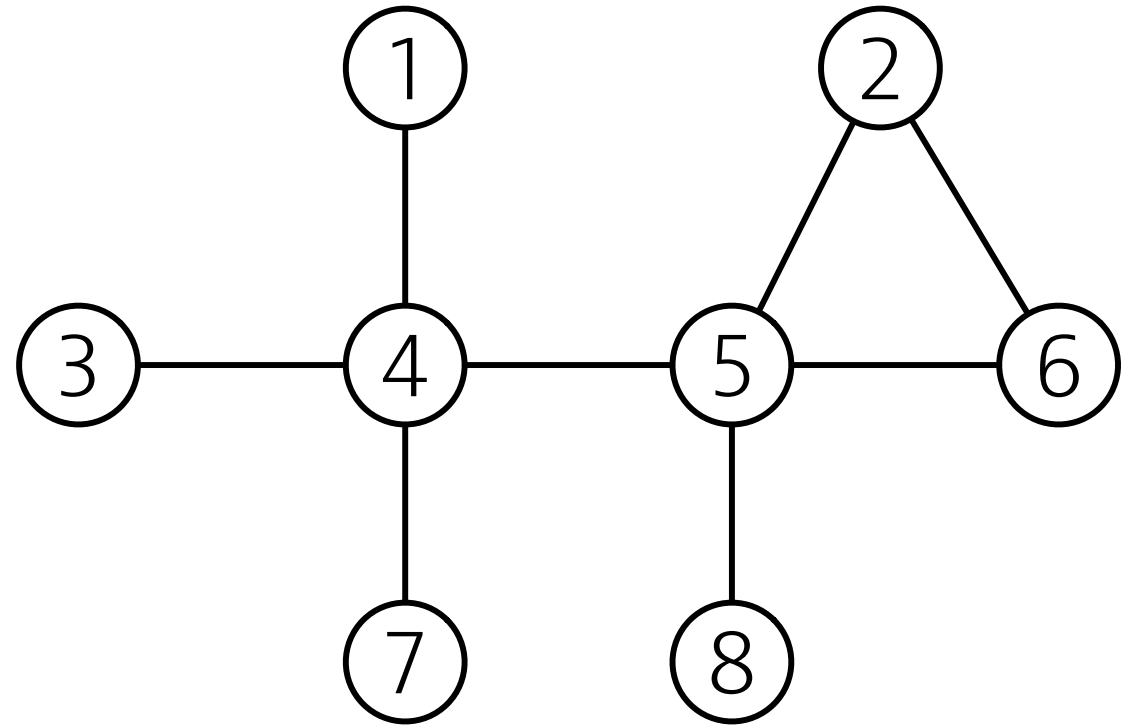


Smallest  
set of nodes  
that is both  
an independent set  
and a dominating set

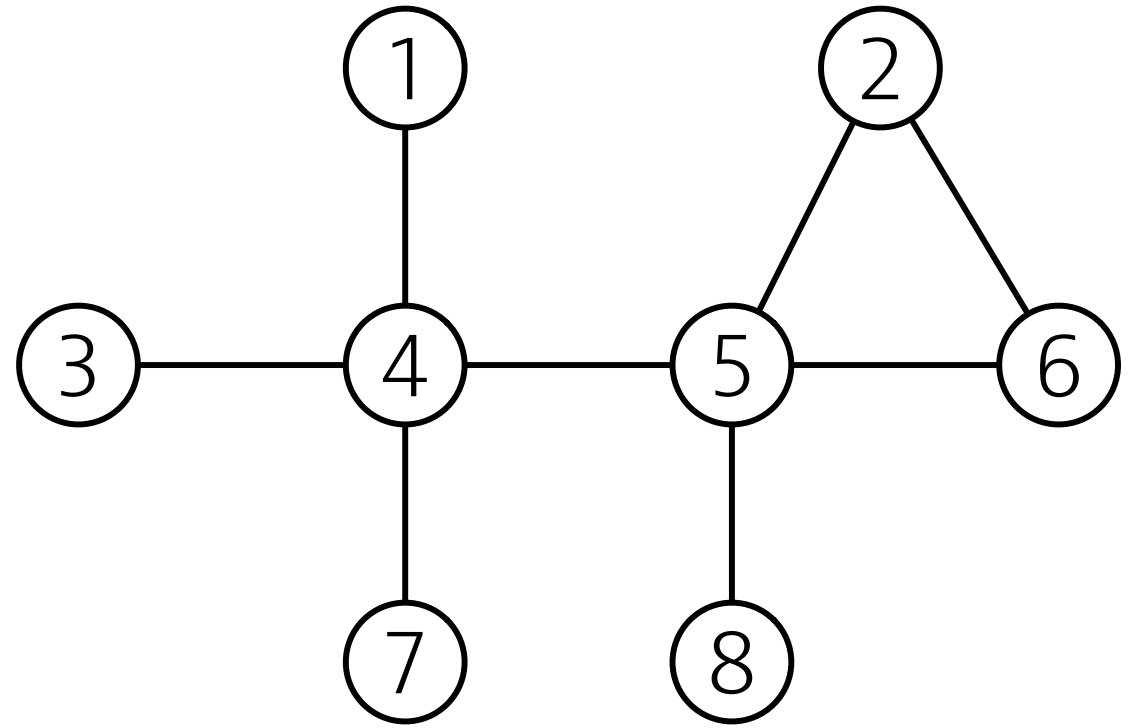


Largest  
set of nodes  
that is both  
an independent set  
and a dominating set

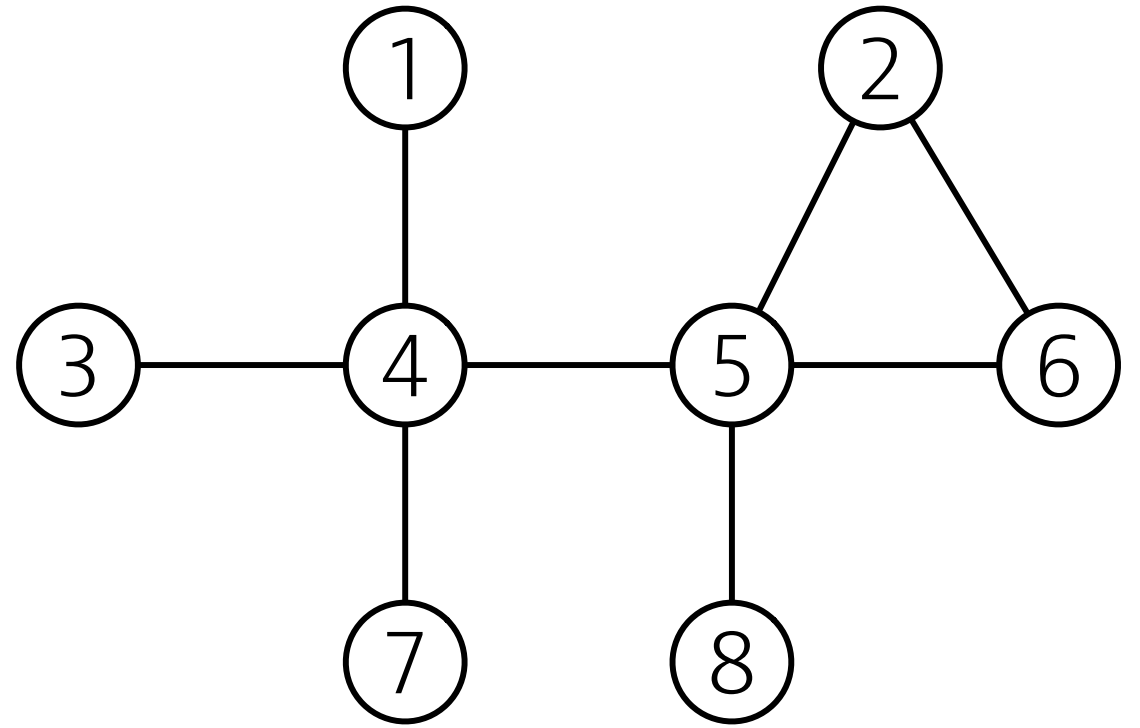




Maximum  
matching



Minimum  
edge cover



Minimum  
edge dominating set