# Distributed Quantum Advantage

When and how does quantum computation and communication speed up problem solving in large computer networks?

Three flavors of quantum advantage in computer networks

#### Communication Local bandwidth computation Less work done **between** Less work done **during** communication steps communication steps Intuition: one quantum computer is more Intuition: extra power that you cannot Intuition: sending one qubit is more useful powerful than one classical computers implement with classical networks, no than sending one classical bit matter how powerful computers you have, no matter how much bandwidth you have! Formalism: quantum-LOCAL Connection Gavoille et al. (DISC 2009): model + first results between distributed and online graph Le Gall et al. (STACS 2019): the first **global** graph problem algorithms with a distributed guantum advantage! But problems studied in distributed graph algorithms are

Key question: is there any *local* graph problem with a distributed guantum advantage?

usually defined with local constraints (e.g. graph coloring)

Quantum can be sandwiched between classical distributed and online!

**ICALP 2023** 

Akbari, Eslami, Lievonen, Melnyk, Särkijärvi, Suomela "Locality in online, dynamic, sequential, and distributed graph algorithms"

Communication

rounds

Smaller **number** of

communication steps

# STOC 2025

Akbari, Coiteux-Roy, d'Amore, Le Gall, Lievonen, Melnyk, Modanese, Pai, Renou, Rozhoň, Suomela "Online locality meets distributed quantum computing"

### STOC 2024

Coiteux-Roy, d'Amore, Gajjala, Kuhn, Le Gall, Lievonen, Modanese, Renou, Schmid, Suomela "No distributed quantum advantage for approximate graph coloring"

## **STOC 2025**

Balliu, Brandt, Coiteux-Roy, d'Amore, Equi, Le Gall, Lievonen, Modanese, Olivetti, Renou, Suomela, Tendick, Veeren "Distributed quantum advantage for local problems"

#### **ICALP 2025**

Balliu, Ghaffari, Kuhn, Modanese, Olivetti, Rabie, Suomela, Uitto "Shared randomness helps with local distributed problems"

No quantum advantage for local problems of the form "c-color k-colorable graphs"

The first local problem with distributed quantum advantage!

Shared randomness helps, and therefore also shared quantum state helps

