

Synthesizing fault-tolerant distributed algorithms

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What is this talk about?

Developing fault-tolerant distributed algorithms for consensus-like problems using computational techniques.

Verification vs synthesis

Verification: "Check that given A satisfies the specification S."

Synthesis:

"Construct an A that satisfies a specification S."

The model problem

The synchronous counting problem:

- Closely related to consensus
- Self-stabilization
- Byzantine fault tolerance
- Hard to come up with correct algorithms

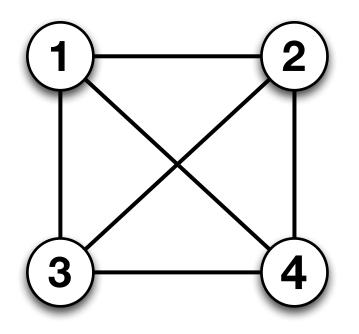
Our work

Prior work: Are there efficient and compact deterministic algorithms? Dolev et al. (SSS 2013)

Recent work: Developing and evaluating different synthesis techniques

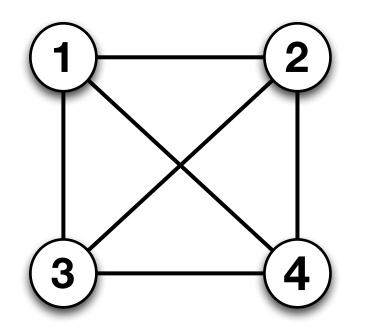
Synchronous counting

The model



- *n* processors
- s states per node
- arbitrary initial state

The model



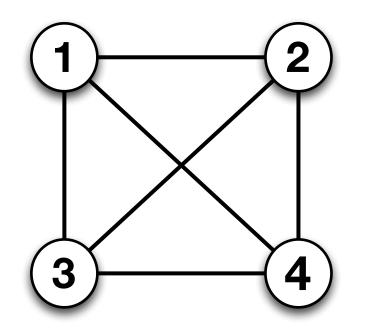
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Synchronous step:

I. send state to all neighbours

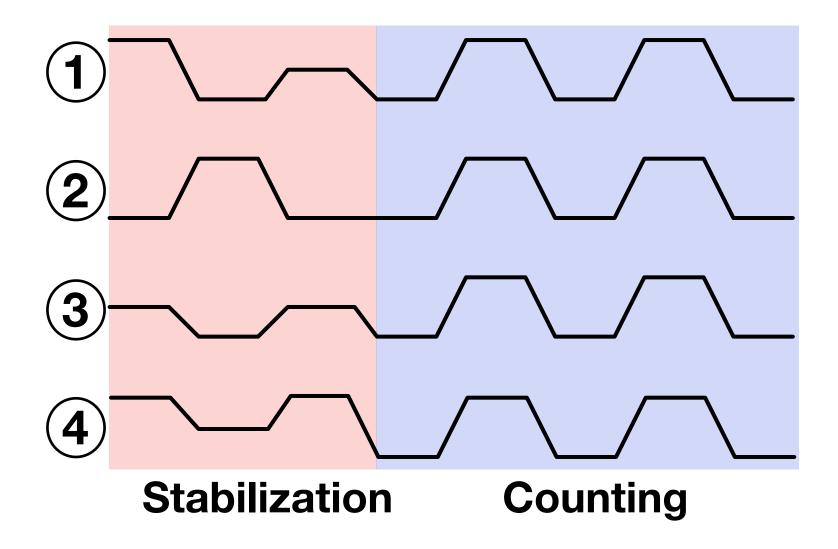
2. update state

The model

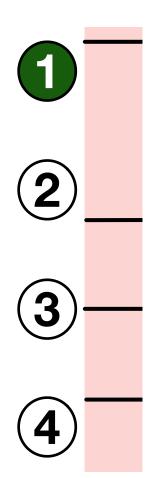


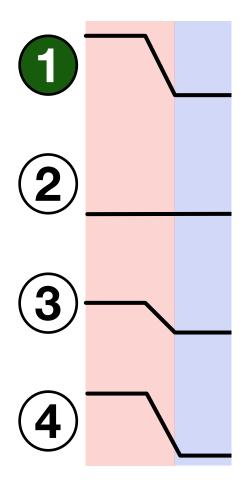
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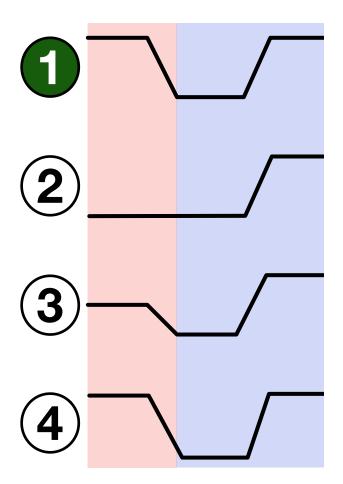
Synchronous step: algorithm
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2. update state

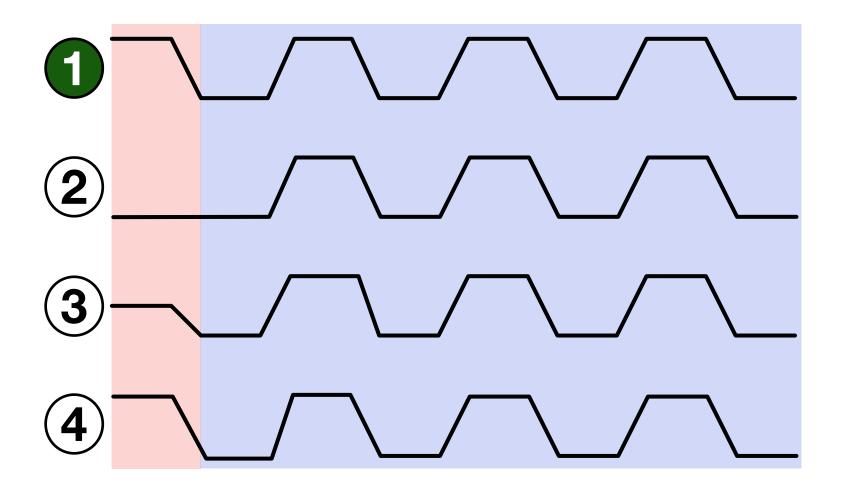


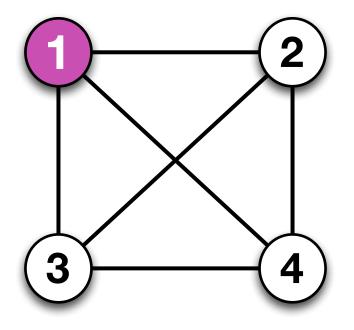
A simple algorithm solves the problem

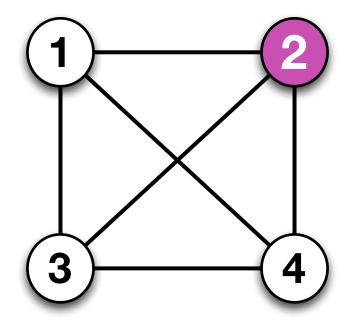


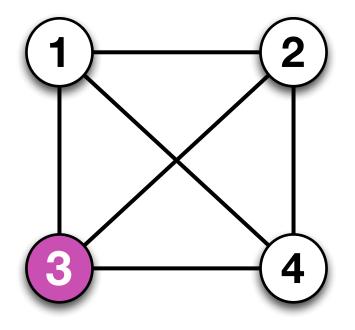


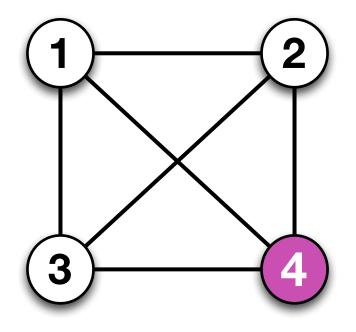


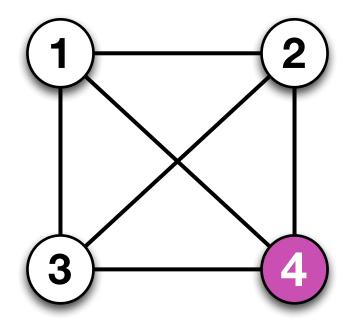






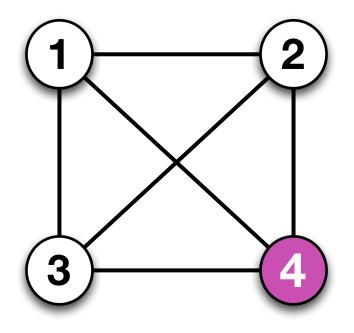


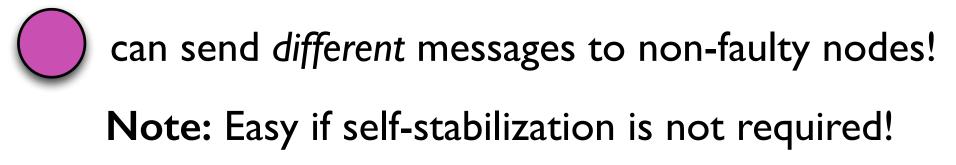




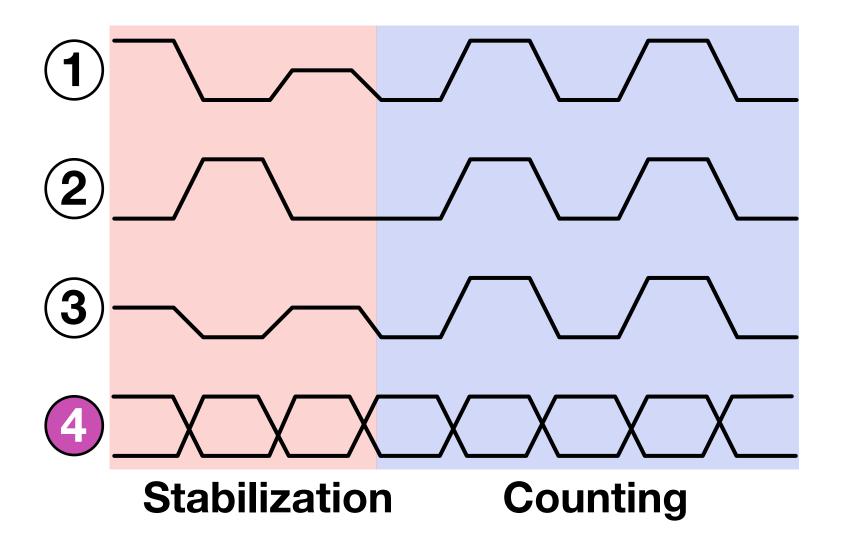


can send different messages to non-faulty nodes!

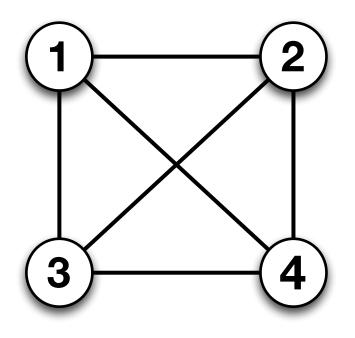




Fault-tolerant counting



The model with failures



- *n* processors
- s states
- arbitrary initial state
- at most *f* Byzantine nodes

Some basic facts

• How many states (per node) do we need?

- s ≥ 2

- How many faults can we tolerate?
 - f < n/3
- How fast can we stabilize?

- t > f

Pease et al., 1980 Fischer & Lynch, 1982

Solving synchronous counting

Deterministic solutions with large s known for similar problems (e.g. D. Dolev & Hoch, 2007)

Randomized solutions for counting with small s and large t in expectation (e.g. S. Dolev: Self-stabilization)

We have synthesized deterministic algorithms with small s and t for the case f = | (SSS'|3)

Finding an algorithm

The size of the search space is s^b where $b = ns^n$.

parameters	search space
n = 4 s = 2	2 ⁶⁴ ≈ 10 ¹⁹

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parameters	search space
n = 4 s = 2	2 ⁶⁴ ≈ 10 ¹⁹
n = 4 s = 3	$3^{324} \approx 10^{154}$

We need a clever way to do the search!

Main results, f = I

If $4 \le n \le 5$:

- lower bound: no 2-state algorithm
- upper bound: 3 states suffice

If $n \ge 6$:

• 2 states always suffice

Synthesis techniques

Our initial approach

- Fix *n*, s and *f*
- The existence of an algorithm is a finite combinatorial decision problem
- Apply SAT solvers to a base case that implies a general solution

Generalizing from a base case

For any fixed s, f and t:

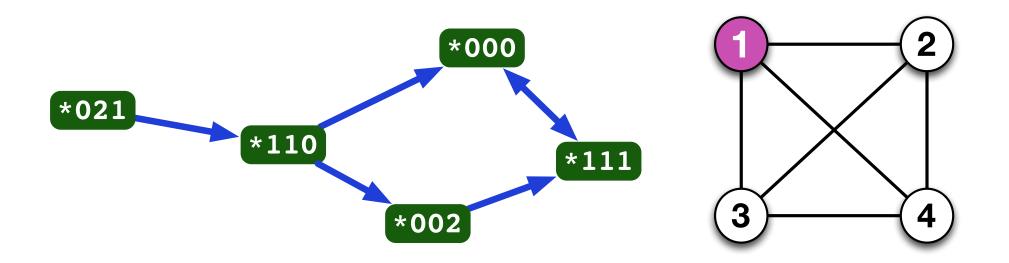
There is an algorithm **A** for *n* nodes

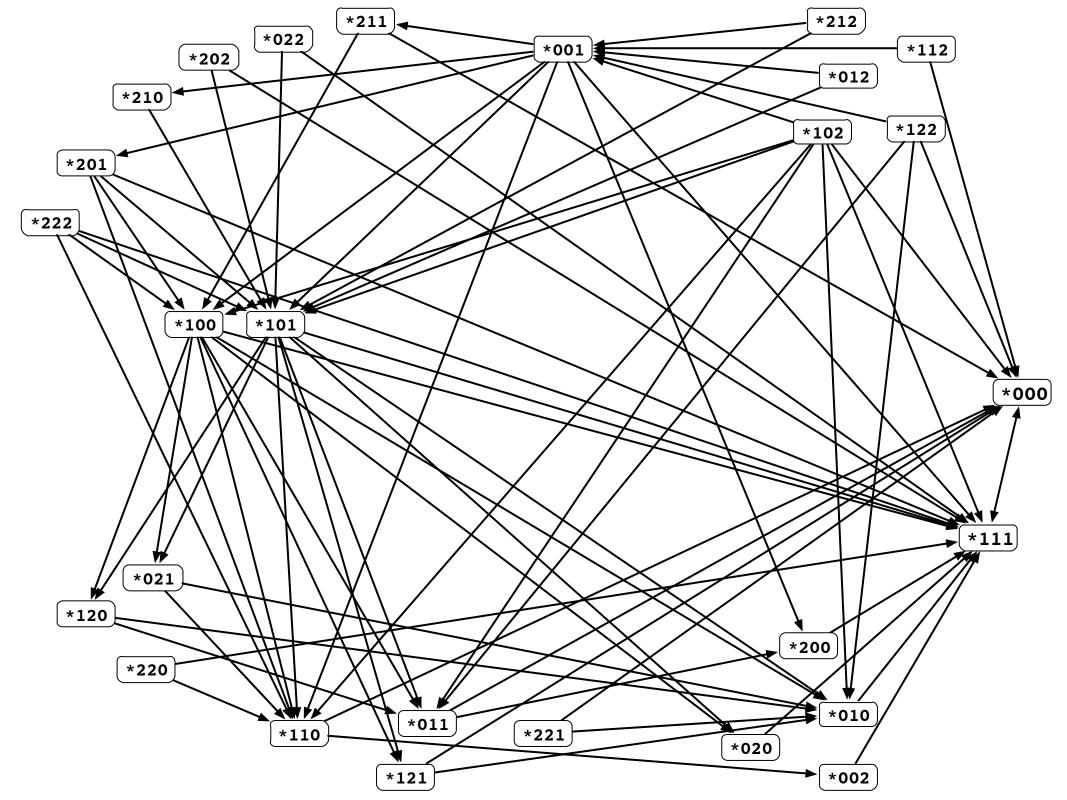


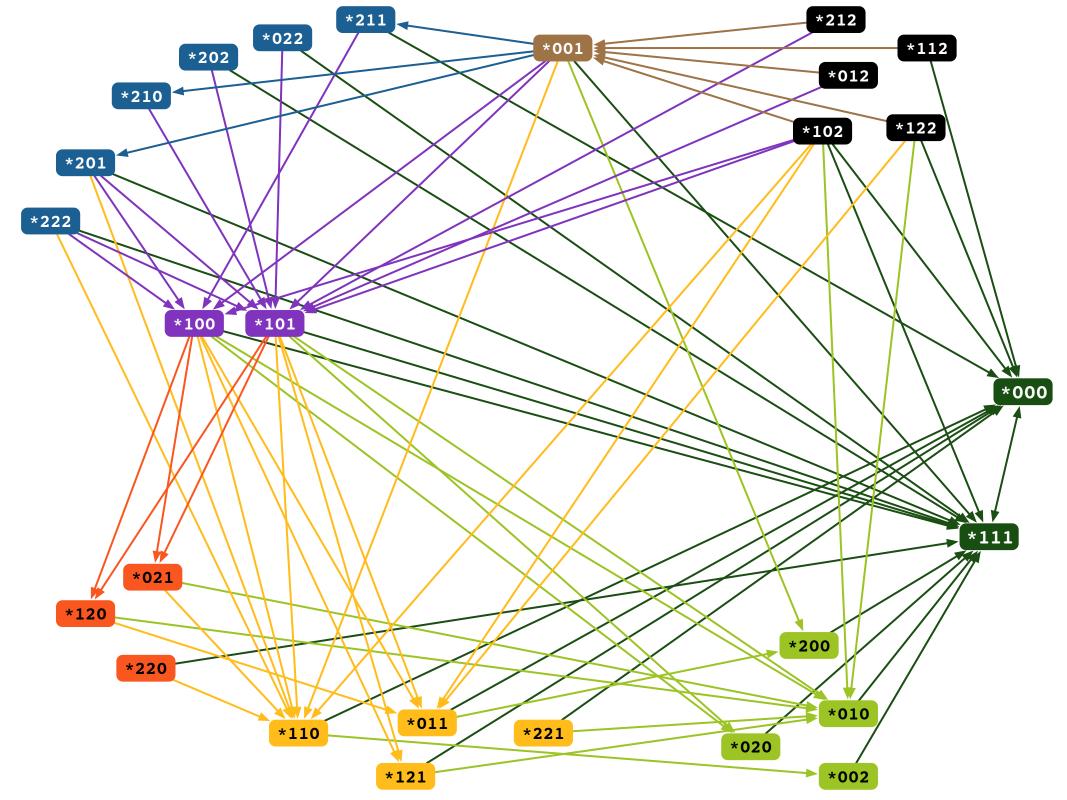
There is an algorithm **B** for *n*+1 nodes with same s, *f* and *t*

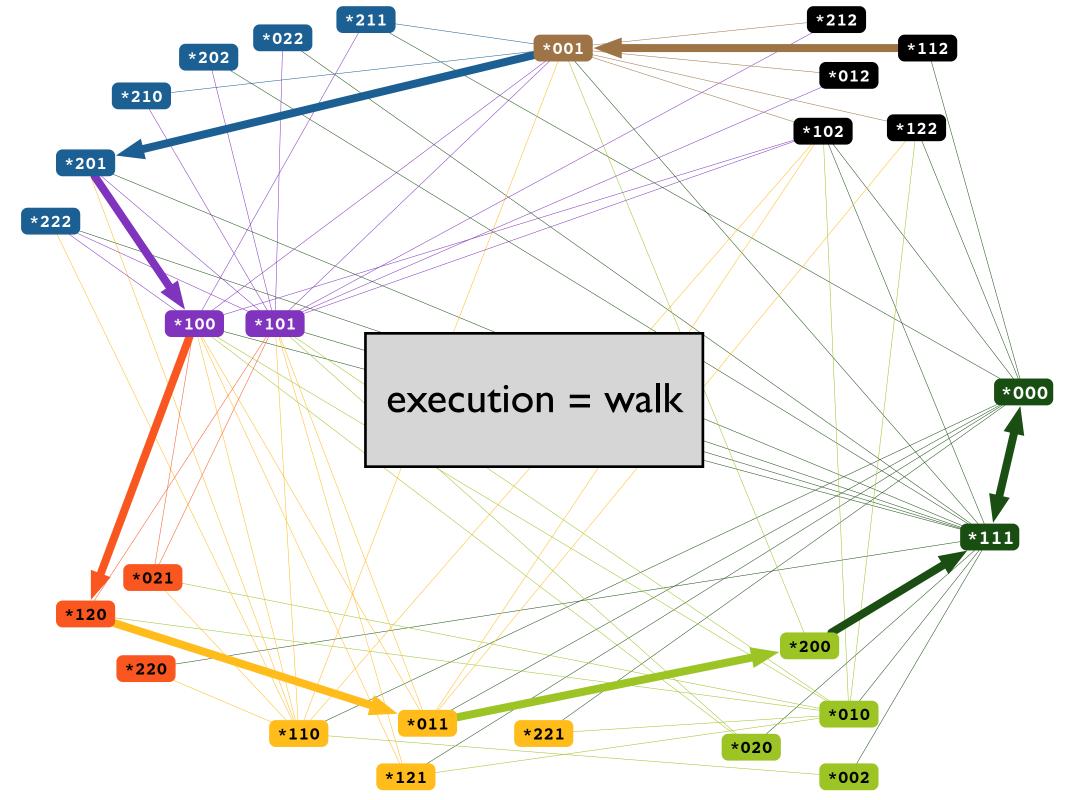
Verification is easy

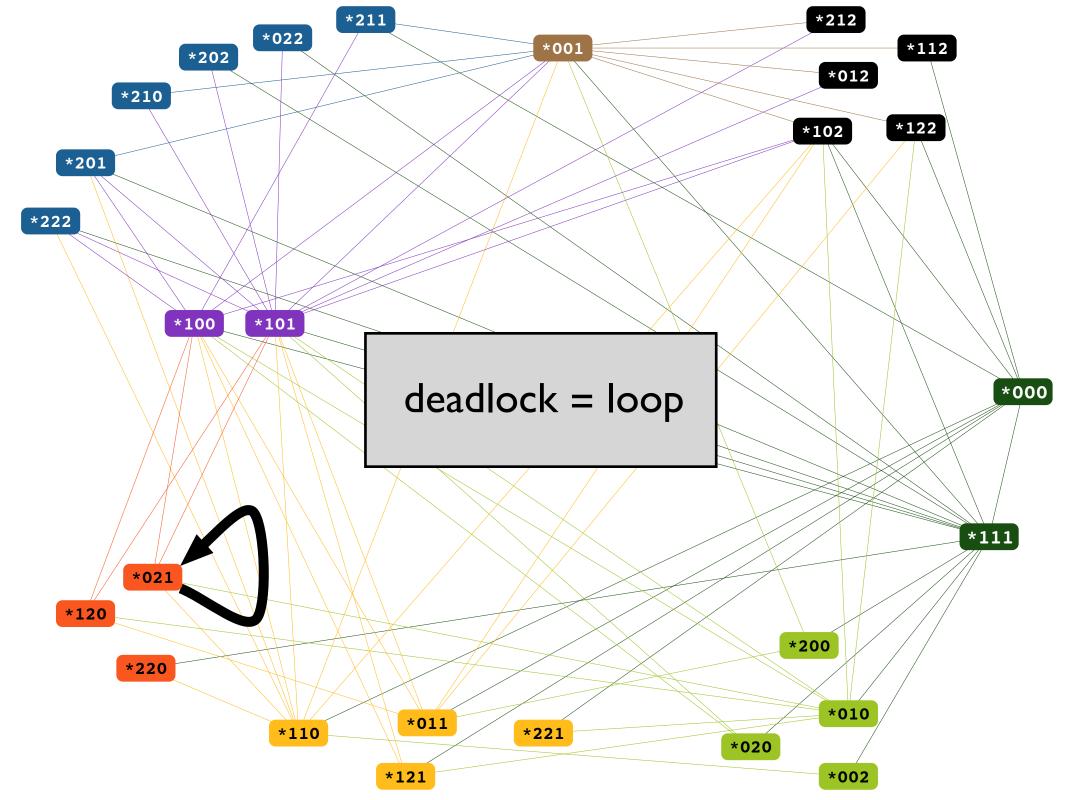
- Let F be a set of faulty nodes, $|F| \leq f$
- Construct a state graph G_F from A:
 Nodes = actual states
 Edges = possible state transitions

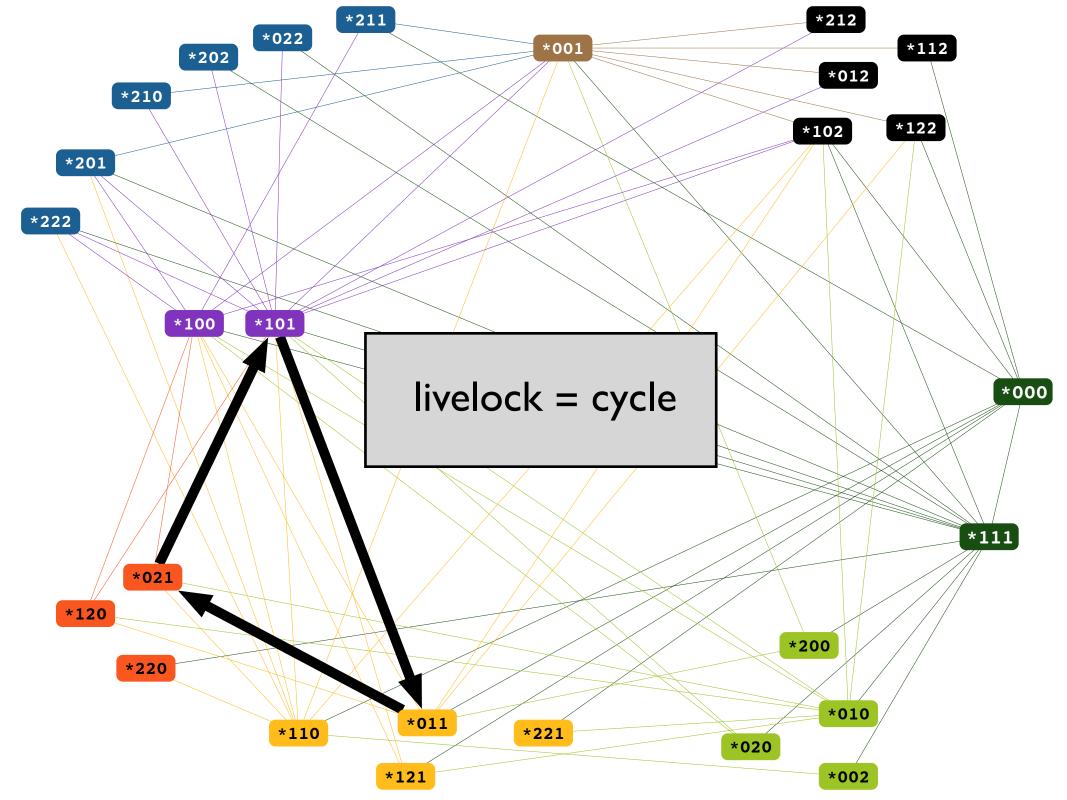


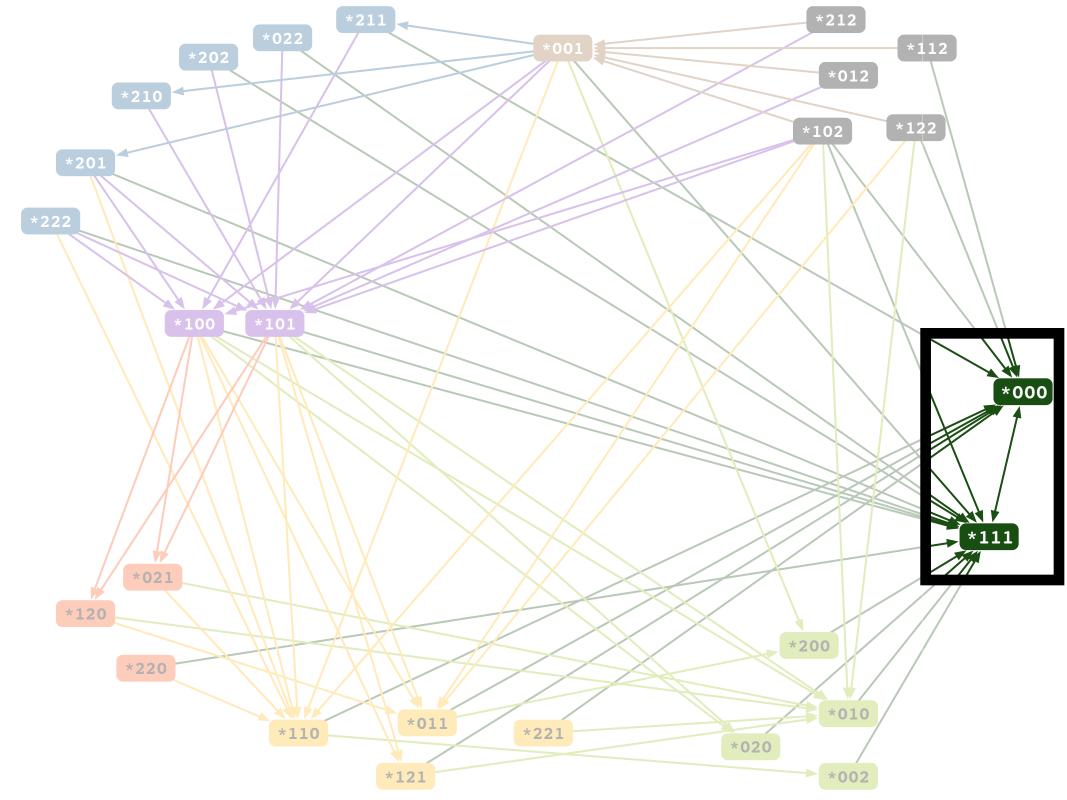


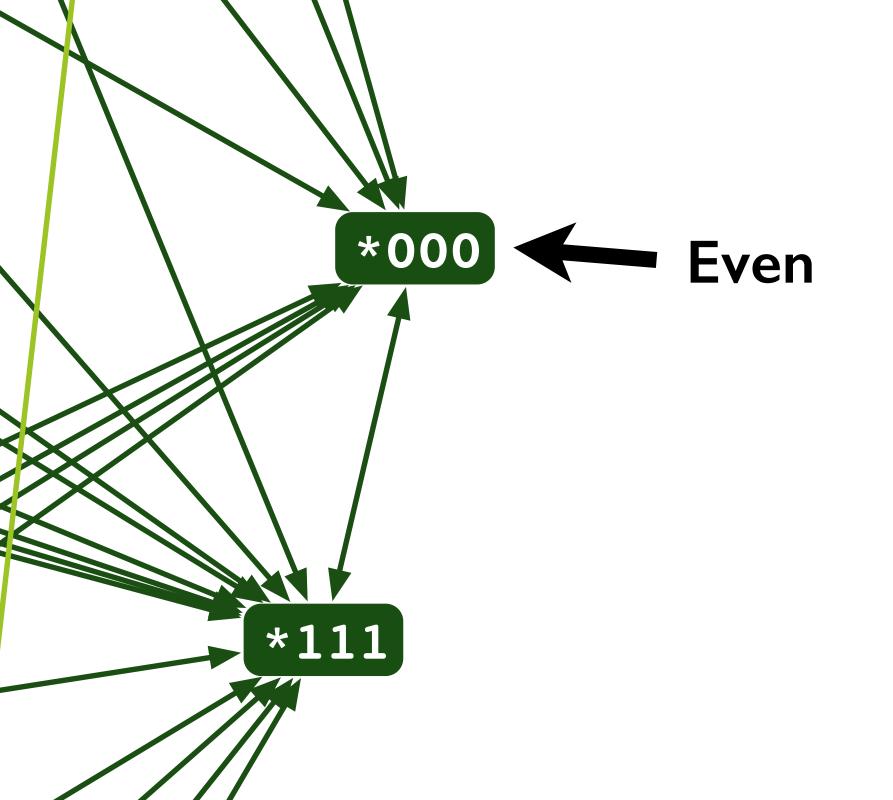


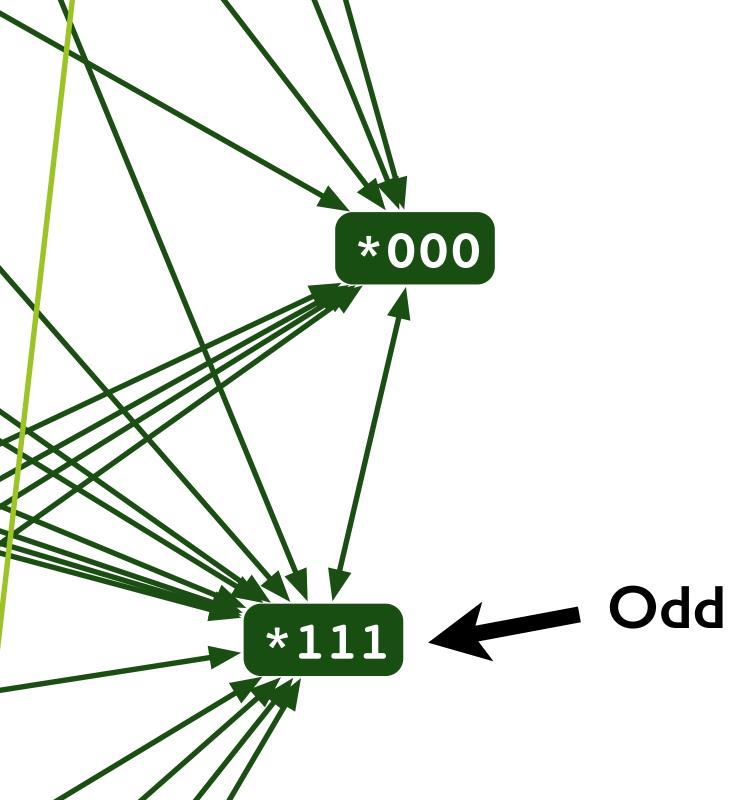












Verification is easy

A is correct \Leftrightarrow Every G_F is good

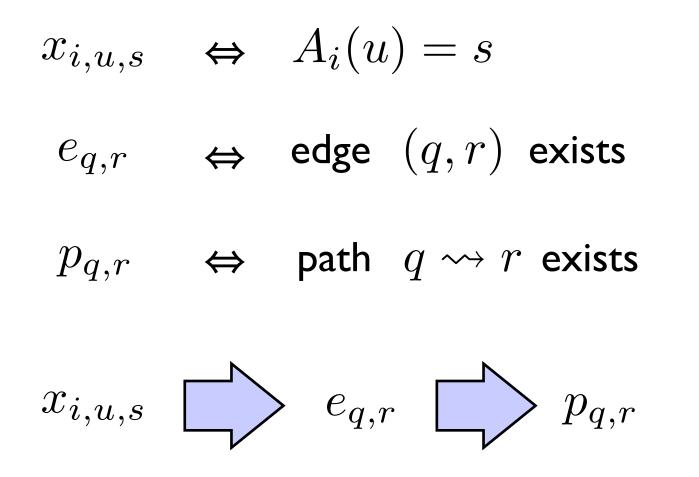
no deadlocks \Leftrightarrow G_F is loopless

stabilization \Leftrightarrow All nodes have a path to **0**

counting $\Leftrightarrow \{0, I\}$ is the only cycle

From verification to synthesis

The encoding uses the following variables:



The SAT approach

- Solver is a black box: no domain-knowledge
- Relatively easy to setup
- Size of instances **blows up**:

The SAT approach

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instance: n, s, t	variables	clauses
4310	6k	31k
5310	45k	36k
6310	403k	4M

Counter-example guided search

- A problem-specific synthesis algorithm
- CEGAR-inspired search
- Uses SAT solver to find *counter-examples*
- Learn constraints on-the-fly

A high-level overview

While algorithm candidates exist:

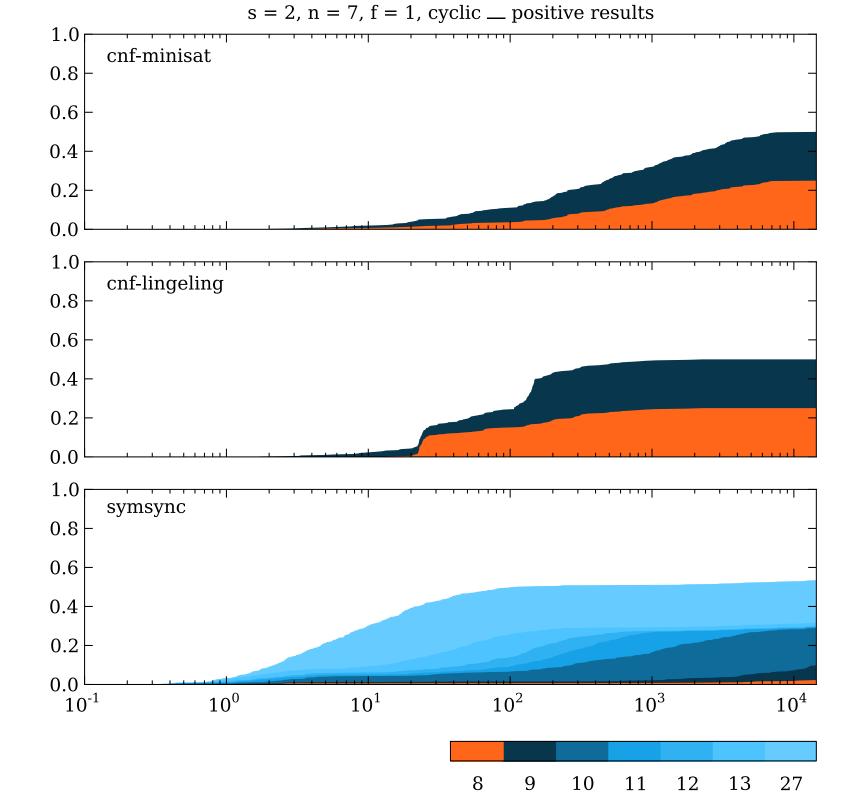
- Guess an algorithm A
- Use a SAT solver to check if A is correct
- If not, solver gives a counter-example. Learn new constraints that forbid bad algorithms

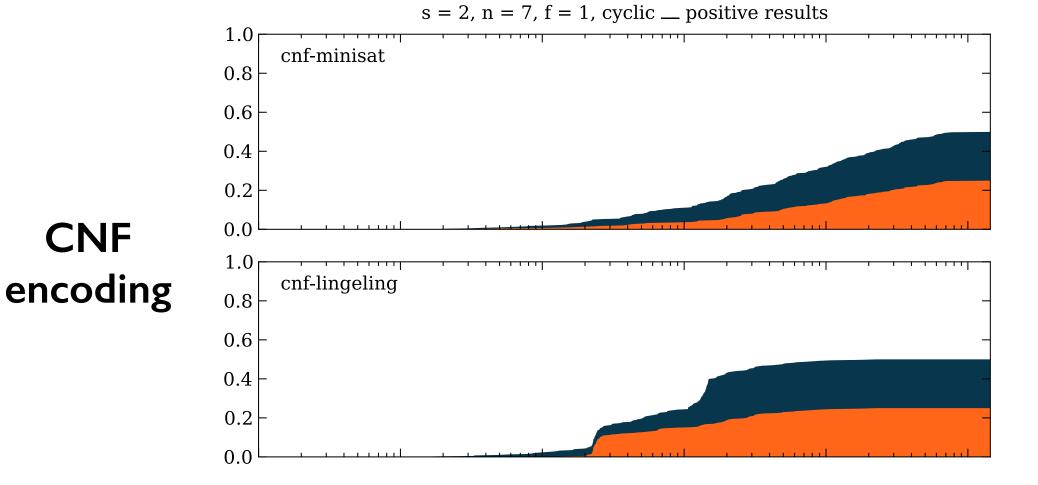
How to learn *useful* constraints from counter-examples?

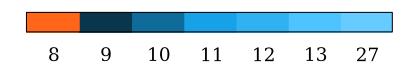
Some experiments

Experiment setup

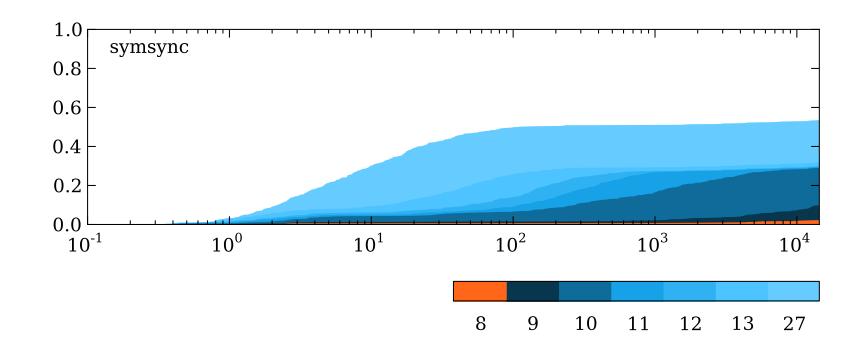
- SAT encoding: MiniSAT and lingeling solvers
- 'symsync': the guided search algorithm
- same instance on 100 processors in parallel, different random seeds

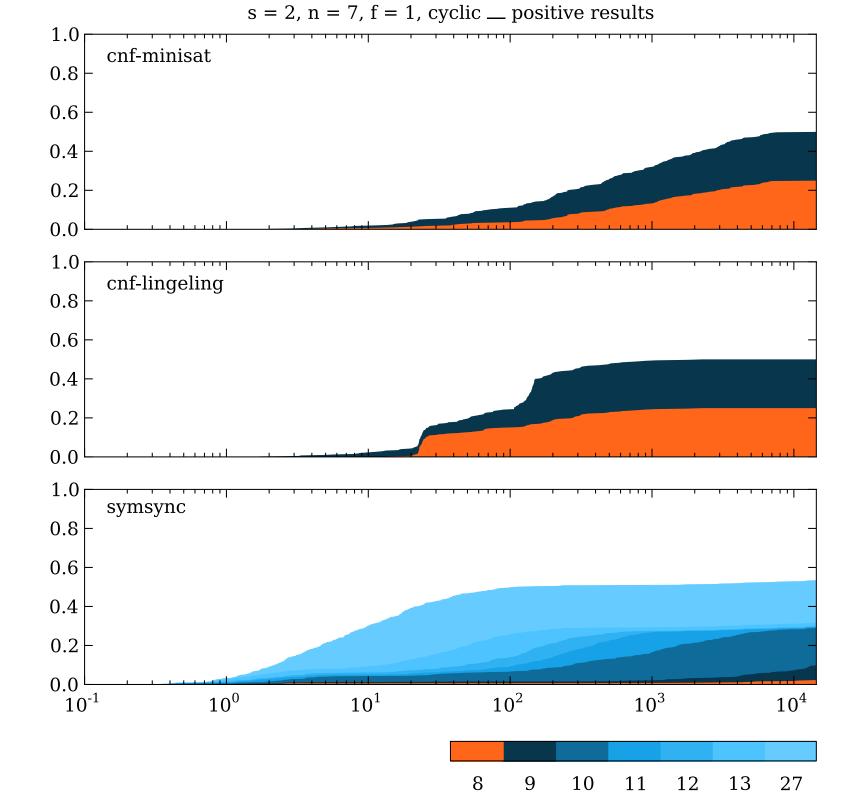


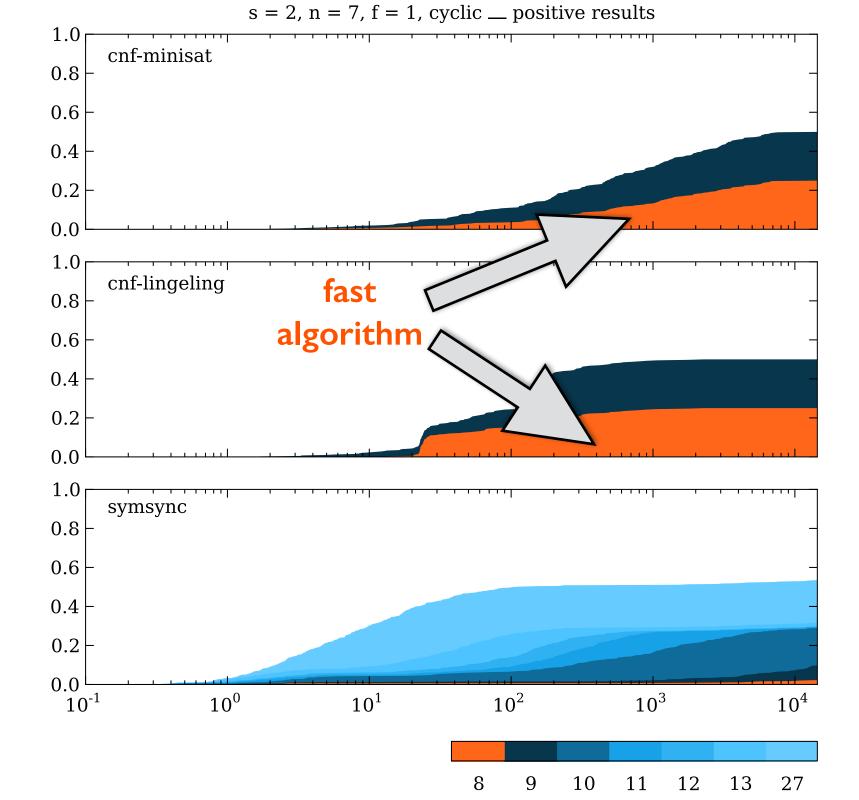


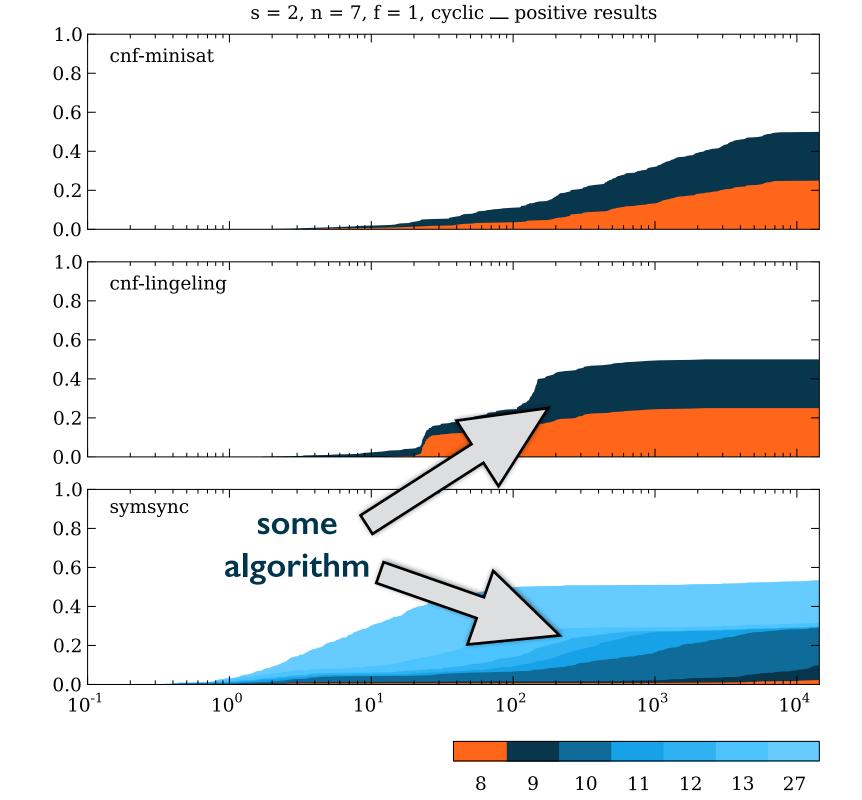


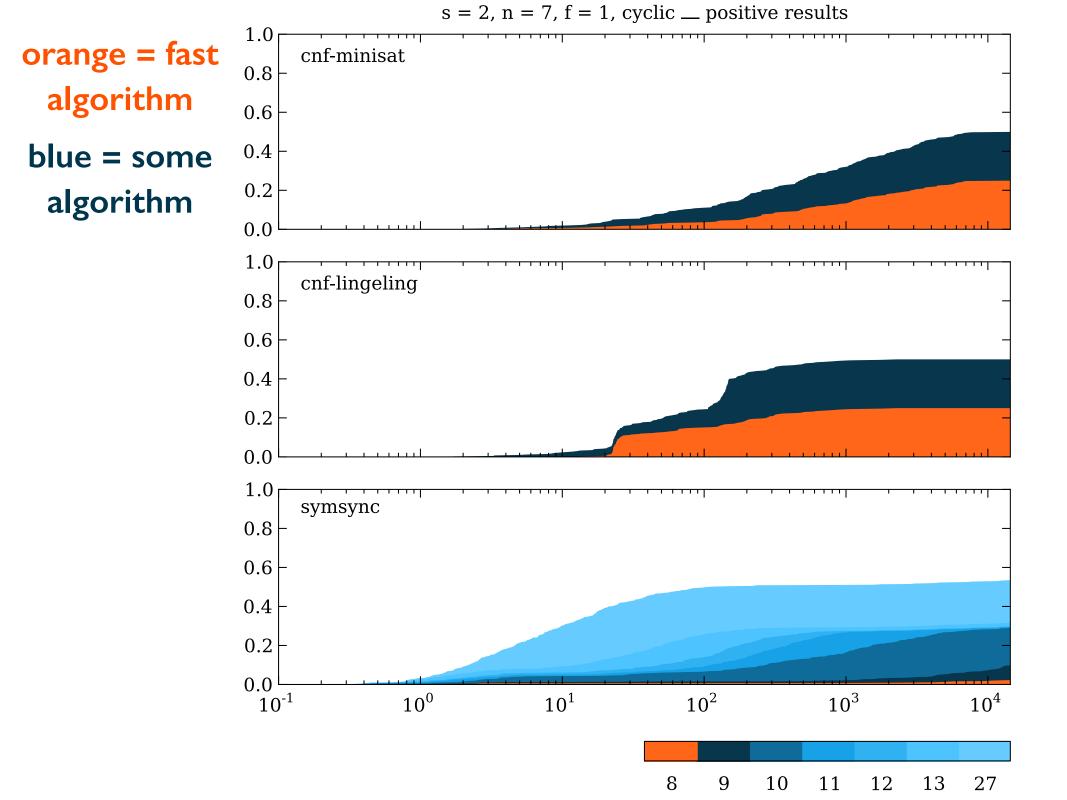


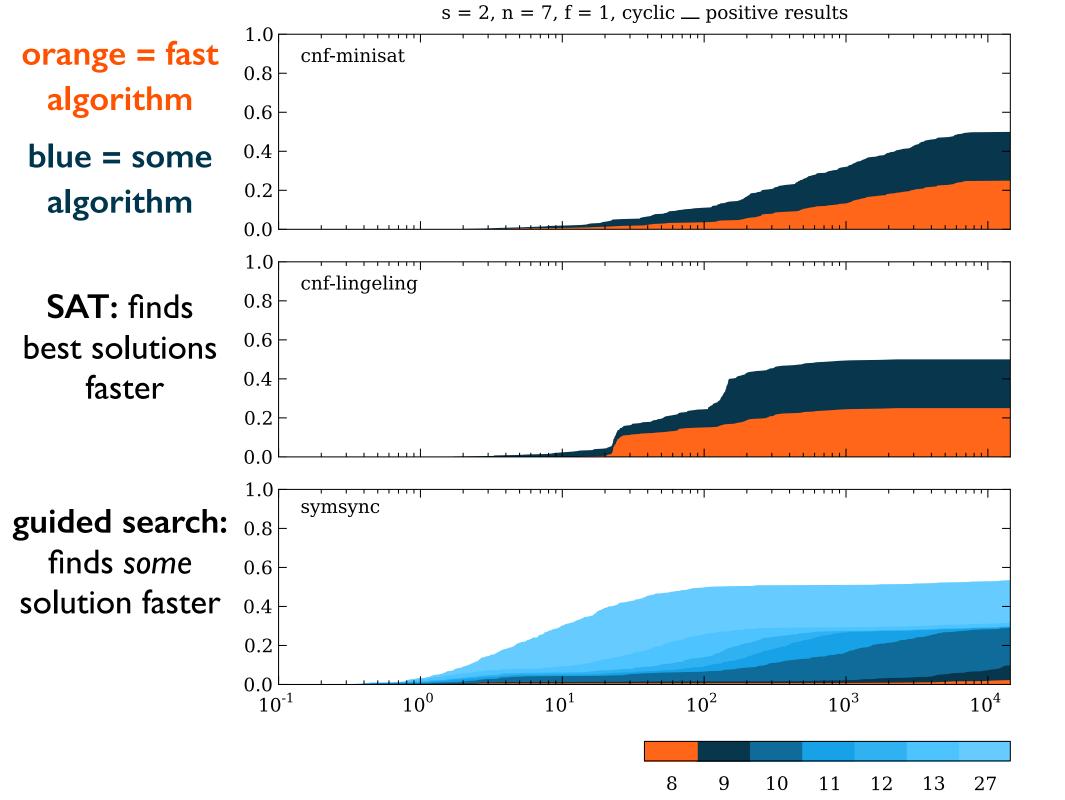


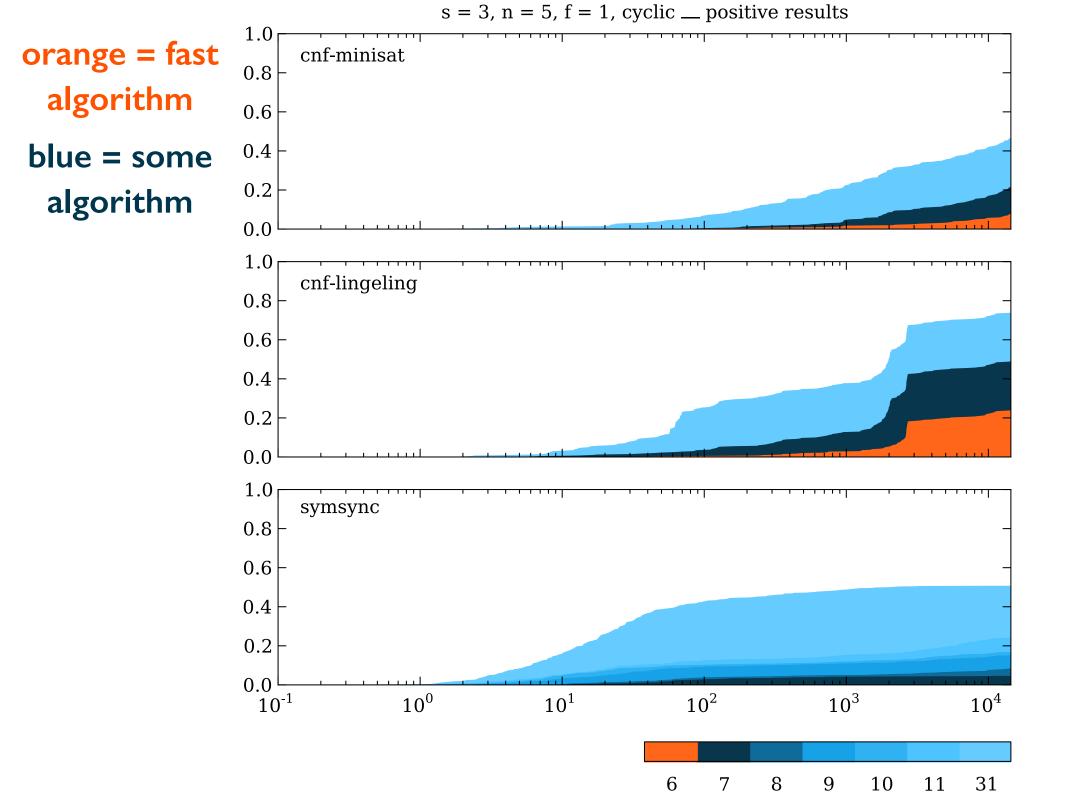


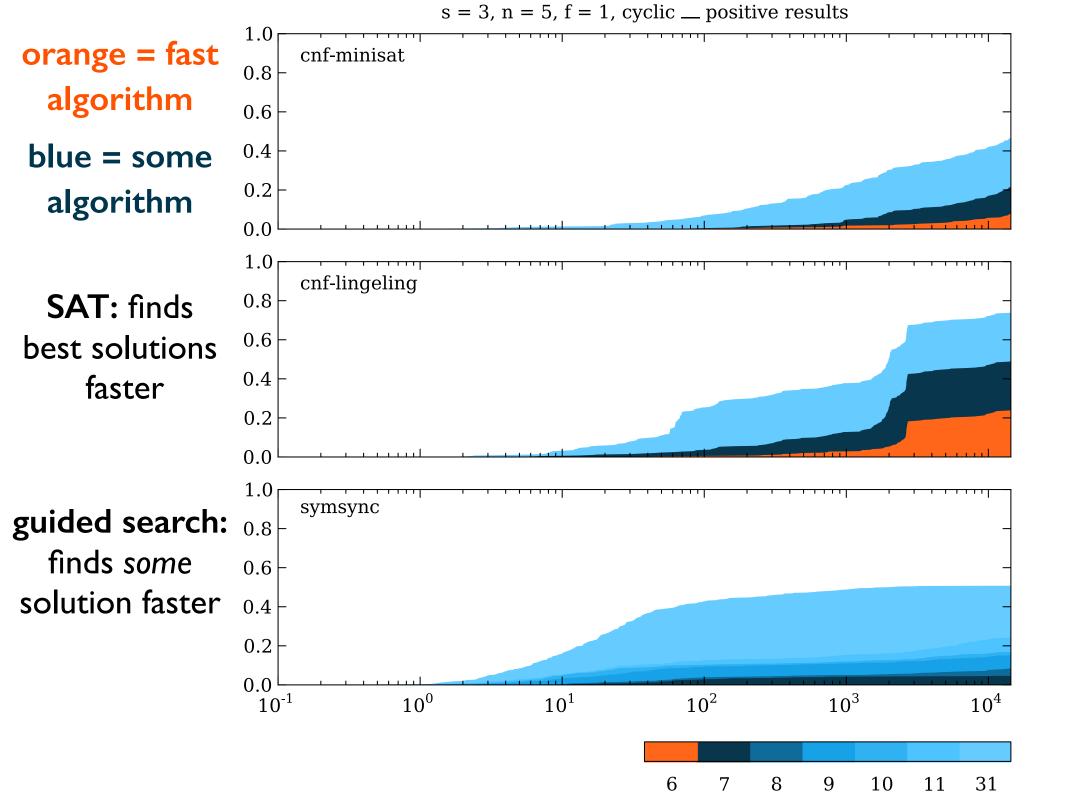


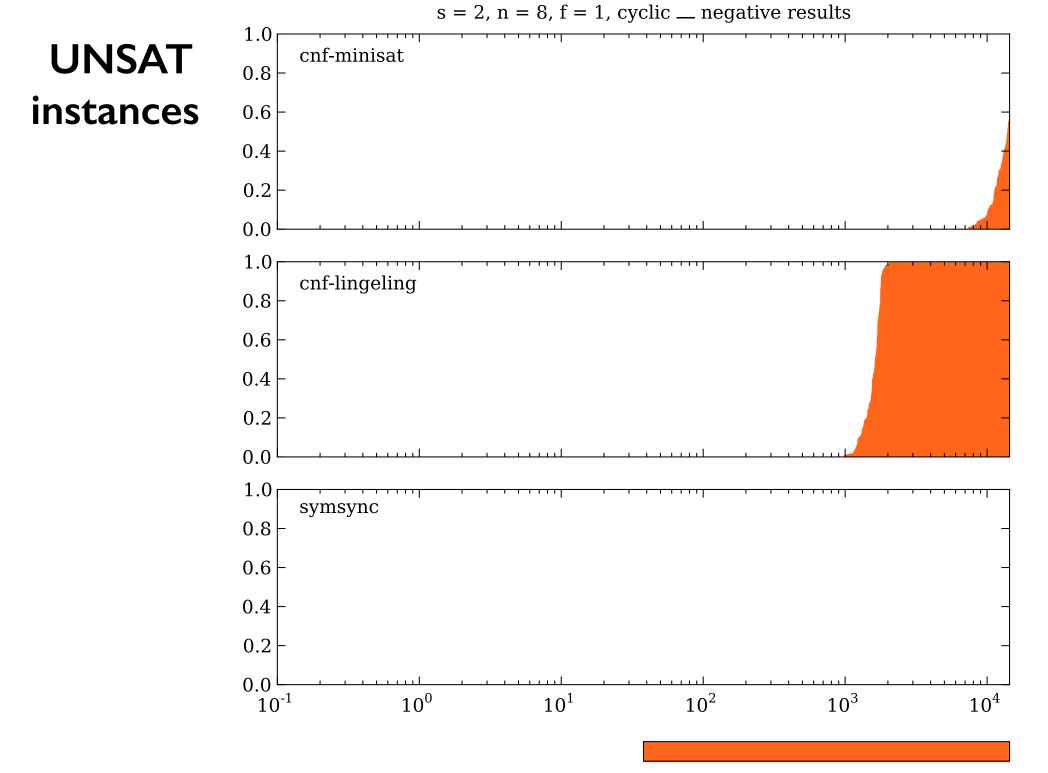












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- Results: optimal fault-tolerant algorithms
- Complementary approaches for fast synthesis

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Thanks!